Investigation of Growth Mechanisms of Clusters in a Silane Discharge With the Use of a Fluid Model

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Abstract—A one-dimensional fluid model was developed to study the formation of dust nanoparticles in a low-pressure capacitively coupled radio-frequency silane (SiH₄) discharge. In this model, the particle balances, the electron energy balance, and the Poisson equation are solved self-consistently. A set of 66 species, including neutrals, radicals, ions, and electrons, are incorporated. A total of 111 reactions are described in the model, comprising electron impact reactions with silanes, neutral-neutral, and ion-neutral reactions. Plasma conditions are typically those used for the deposition of amorphous silicon (a-Si:H). The model includes the formation of silicon hydrides (Si_nH_m) containing up to 12 silicon atoms. Anion-induced chain reactions are considered to be the main pathway leading to cluster formation.

Index Terms—Dusty silane plasma, nucleation.

I. INTRODUCTION

ARTICLE formation in low-pressure silane discharges, creating "dusty" plasmas, has gained substantial interest over the past years [1]-[4]. Indeed, the presence of dust in industrial plasma reactors can lead to the production of defective films if the particles are incorporated into the film during the plasma-enhanced chemical vapor deposition (PECVD) process [5], [6]. On the other hand, solar cell application seems to benefit from the presence of nanometer-size particles in the amorphous silicon layer (a-Si:H), as an increase in the performance of the solar cell is observed [7], [8]. Hence, understanding the origin and the behavior of these particles can help in finding efficient ways to minimize, or to eliminate, undesirable particles in the microelectronics, as well as enhance the embedded particles to improve film properties. Comprehension of these aspects advances the development of both fundamental knowledge and potential applications.

Here, we study the initial mechanism by which silicon particles start growing, which is experimentally the most difficult stage to observe due to the very small size of the particles ($r_p < 5$ nm) requiring sophisticated diagnostics [9]. Therefore, theoretical models can provide an alternative. Investigations [5], [10] have shown that particles are formed due to successive reactions in the gas phase, known as gas phase polymerization, and the surface is not believed to play any role in the production

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process. Negative ions are generally considered to be the particle precursors, since they are trapped in the plasma bulk and have a longer residence time in the plasma [11]–[13]. Reactions with negative ions are therefore considered as the primary clustering pathway in our simulations.

A description of the model, including the plasma kinetics, is presented in Section II. In Section III, results of the various simulations are represented and discussed. Finally, the conclusion is given in Section IV.

II. MODEL DESCRIPTION

A. Fluid Model

The model for describing the nucleation of dust in silane plasmas is based on the fluid model developed by Nienhuis *et al.* [14] for the description of a silane/hydrogen discharge.

This fluid model describes the discharge by a combination of particle, momentum, and energy density balances of the ions, electrons, and neutrals. The balance equations are coupled to the Poisson equation for the calculation of the electric field. Typical discharge quantities such as the electric field, densities, and fluxes of the particles as a function of space and time are calculated self-consistently. An overview of the model can be found elsewhere [14], [15]. The system of nonlinear differential equations is solved numerically. For the spatial discretization of the balance equations, the Scharfetter-Gummel exponential scheme is used [16]. The computational grid is equidistant and contains 64 grid points. An implicit second-order method [17] is applied to numerically treat the time evolution of the balance equations. Finally, the Newton-Raphson method is used to solve the resulting set of nonlinear equations. Convergence of the fluid model is reached when the relative changes of the discharge parameters between two succeeding radio-frequency (RF) cycles are less than 10^{-6} . Further details concerning the numerical techniques and algorithms can be found in [17] and [18].

No secondary electrons are taken into account, so the results are limited to the α -regime of a capacitively coupled RF discharge. This is a good estimate since the results are computed at low pressures (order of several hundred mtorr) and power (5 W) where the RF discharge is assumed to operate in the alfa regime [19], [20]. Power input into the plasma is transferred to the charged species (electrons and ions) by ohmic heating.

B. Plasma Kinetics

A basic set of reactions has been taken from Nienhuis *et al.* [14] for a silane discharge without the inclusion of nanoparticles. A series of chemical reactions has been gradually incor-

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Molecules	Ions	Radicals
SiH ₄	SiH_3^+ , $\operatorname{Si}_2\operatorname{H}_4^+$, SiH_3^- , SiH_2^-	SiH ₃ , SiH ₂
H ₂	H_2^+	Н
Si ₂ H ₆ , Si ₃ H ₈ , Si ₄ H ₁₀ , Si ₅ H ₁₂	$Si_2H_5^-$, $Si_3H_7^-$, $Si_4H_9^-$, $Si_5H_{11}^-$	Si ₂ H ₅ , Si ₃ H ₇ , Si ₄ H ₉ , Si ₅ H ₁₁
Si ₆ H ₁₄ , Si ₇ H ₁₆ , Si ₈ H ₁₈ , Si ₉ H ₂₀	$Si_6H_{13}^-$, $Si_7H_{15}^-$, $Si_8H_{17}^-$, $Si_9H_{19}^-$	Si_6H_{13} , Si_7H_{15} , Si_8H_{17} , Si_9H_{19}
Si ₁₀ H ₂₂ , Si ₁₁ H ₂₄ , Si ₁₂ H ₂₆	$Si_{10}H_{21}^-$, $Si_{11}H_{23}^-$, $Si_{12}H_{25}^-$	Si ₁₀ H ₂₁ , Si ₁₁ H ₂₃ , Si ₁₂ H ₂₅
	$Si_2H_4^-$, $Si_3H_6^-$, $Si_4H_8^-$, $Si_5H_{10}^-$	Si_2H_4 , Si_3H_6 , Si_4H_8 , Si_5H_{10}
	$Si_6H_{12}^-$, $Si_7H_{14}^-$, $Si_8H_{16}^-$, $Si_9H_{18}^-$	Si_6H_{12} , Si_7H_{14} , Si_8H_{16} , Si_9H_{18}
	$Si_{10}H_{20}^-$, $Si_{11}H_{22}^-$, $Si_{12}H_{24}^-$	Si ₁₀ H ₂₀ , Si ₁₁ H ₂₂ , Si ₁₂ H ₂₄

 TABLE I

 DIFFERENT SPECIES TAKEN INTO ACCOUNT IN THE MODEL, BESIDES THE ELECTRONS

 TABLE II

 ELECTRON IMPACT COLLISIONS USED IN THE MODEL

	Reaction	Reaction type	Reference
1.	$\operatorname{SiH}_4 + e^- \rightarrow \operatorname{SiH}_3^+ + H + 2e^-$	dissociative ionization	[22]
2.	$\mathrm{Si}_{2}\mathrm{H}_{6} + \mathrm{e}^{-} \rightarrow \mathrm{Si}_{2}\mathrm{H}_{4}^{+} + 2\mathrm{H} + 2\mathrm{e}^{-}$	dissociative ionization	[22]
3.	$SiH_4^{(0)} + e^- \rightarrow SiH_4^{(\bar{2}-4)} + e^- \rightarrow SiH_4^{(0)} + e^-$	vibrational excitation	[23]
4.	$\operatorname{SiH}_{4}^{(0)} + e^{-} \rightarrow \operatorname{SiH}_{4}^{(1-3)} + e^{-} \rightarrow \operatorname{SiH}_{4}^{(0)} + e^{-}$	vibrational excitation	[23]
5.	$SiH_4 + e^- \rightarrow SiH_3 + H + e^-$	dissociation	[24], [25]
6.	$\mathrm{SiH}_4 + \mathrm{e}^- \rightarrow \mathrm{SiH}_2 + 2\mathrm{H} + \mathrm{e}^-$	dissociation	[24], [25]
7.	$Si_2H_6 + e^- \rightarrow SiH_3 + SiH_2 + H + e^-$	dissociation	[24]
8.	$SiH_4 + e^- \rightarrow SiH_3^- + H$	dissociative attachment	[26]
9.	$SiH_4 + e^- \rightarrow SiH_2^- + 2H$	dissociative attachment	[26]
10.	$\mathrm{H}_2 + \mathrm{e}^- \rightarrow \mathrm{H}_2^+ + \bar{2}\mathrm{e}^-$	ionization	[27]
11.	$H_2 + e^- \rightarrow H_2^{(v=1)} + e^-$	vibrational excitation	[28]
12.	$H_2 + e^- \rightarrow H_2^{(v=2)} + e^-$	vibrational excitation	[28]
13.	$H_2 + e^- \rightarrow H_2^{(\upsilon=3)} + e^-$	vibrational excitation	[28]
14.	$H_2 + e^- \rightarrow H^+ H + e^-$	dissociation	[29]

porated, starting from silane leading to the formation of larger silicon hydrides, mostly through the anion pathway. Silicon hydrides containing up to 12 silicon atoms are included. A sensitivity study has been performed in order to obtain a minimum set of different species and reactions, which still gives a reasonable picture of the growth process. When a species or reaction has a negligible influence on the overall plasma chemistry, it is removed from the calculations. Examples are given below.

Table I gives an overview of the different species considered in our model, besides the electrons. The inlet gas SiH₄ will of course play an important role in the plasma and will be present at the highest density. Vibrationally excited silane species are not represented by separate species in this model, in order to reduce the computational effort. Electron reactions leading to vibrational excitation are, however, included, where the vibrationally excited molecules are treated as ground state molecules, thus not requiring their separate incorporation (see Table II). Higher order silanes (Si_nH_{2n+2}), especially disilane, are incorporated, as they take part in the cluster formation and are present at relatively high densities. If a species Si_nH_{2n+2} is included, then it is also necessary to include the radical Si_nH_{2n+1} , since the H abstraction reactions are considered to be important (see Table III). In addition to the silanes, the silylenes (Si_nH_{2n}) have to be incorporated, mainly because their corresponding anions represent a possible clustering route. Silvlenes are isomers of silenes (i.e., molecules with a double bond between two silicon atoms) but with a single bond between the two silicon atoms and with two nonbonding electrons. They are considered to be reactive, thus we classify them as radicals. Although silylenes can isomerize to silenes, which are thermodynamically more stable, the silenes are not considered in our model, because they are chemically inactive and will only accumulate in the reactor at relatively low densities. Silyl anions $(Si_nH_{2n+1}^-)$ and silylene anions $(Si_nH_{2n}^-)$ up to 12 silicon atoms are also taken into account, because the growth of clusters occurs mainly through the anion pathway [12], [21] making them the most prominent particles to include in the simulations. No distinction was made between linear and cyclic molecules.

Table II outlines the electron reactions taken into account. The rate constants of the electron-induced reactions depend strongly on the electron energy distribution function, which is obtained from the two-term expansion of the Boltzmann equation. Rate coefficients as a function of the average electron energy are introduced into the fluid model. The references for the cross section data for the ionization, dissociation, attachment, and vibrational excitation of silane, and in some cases of disilane and hydrogen, are indicated in Table II. Dissociation of silane leads mostly to SiH₃ and SiH₂ radicals with a branching ratio of 0.17/0.83 for SiH₃/SiH₂ [24]. Although ionization can lead to a number of positive ions, the ionization cross sections of Si₂H₆, SiH₄, and H₂ have been lumped and attached to the ion which is most likely formed, i.e., $Si_2H_4^+$, SiH_3^+ , and H_2^+ , respectively. For dissociative attachment of SiH₄, a similar procedure has been used. Only SiH₃⁻ and SiH₂⁻ are considered to be the most abundant anions formed by dissociative attachment of SiH₄, with over 70% leading to the formation of SiH₃.

	Reaction	Rate constant $(m^3 s^{-1})$	Comment		Ref.			
Hyd	Hydrogen abstraction							
1.	$SiH_4 + H \rightarrow SiH_3 + H_2$	1.2×10^{-18}	$2.8 \times 10^{-17} \exp(-$	$-1250/\mathrm{T_{gas}})$	[36], [37]			
2.	$Si_2H_6 + H \rightarrow Si_2H_5 + H_2$	$7.0 imes 10^{-18}$	$1.6 \times 10^{-16} \exp(-1.6 \times 10^{-16})$	$-1250/T_{gas})$	[36], [37]			
3.	$Si_2H_6 + H \rightarrow SiH_3 + SiH_4$	3.5×10^{-18}	$0.8 \times 10^{-16} \exp(-$	$-1250/\mathrm{T_{gas}})$	[36], [37]			
4.	$\mathrm{Si}_{n}\mathrm{H}_{2n+2} + \mathrm{H} \rightarrow \mathrm{Si}_{n}\mathrm{H}_{2n+1} + \mathrm{H}_{2}$	1.1×10^{-17}	$2.4 \times 10^{-16} \exp(-$	$-1250/T_{gas})$ n=3,,12	[36], est.			
Clus	ster growth through SiH_2 insertion							
5.	$SiH_2 + H_2 \rightarrow SiH_4$	$2.7 imes10^{-20}$	$3.0 \times 10^{-18} [1 - ($	$1 + 2.3 \times 10^{-4} \mathrm{p}_0)^{-1}$]	[36]			
6.	$SiH_2 + SiH_4 \rightarrow Si_2H_6$	2.3×10^{-17}	$2.0 \times 10^{-16} [1 - ($	$1 + 0.0032 p_0)^{-1}$]	[36]			
7.	$\mathrm{SiH}_2 + \mathrm{Si}_n\mathrm{H}_{2n+2} \to \mathrm{Si}_{n+1}\mathrm{H}_{2n+4}$	4.9×10^{-17}	$4.2 \times 10^{-16} [1 - ($	$(1 + 0.0033 p_0)^{-1}]$	[36]			
Oth	er neutral-neutral reactions			n=2,,.				
8.	$Si_2H_5 + Si_2H_5 \rightarrow Si_4H_{10}$	1.5×10^{-16}			[36], est.			
9.	$SiH_3 + SiH_3 \rightarrow SiH_2 + SiH_4$	1.5×10^{-16}			[36], [38]			
Clus	ster growth through silyl anions $(Si_nH_{2n+1}^-)$ w	ith silane						
10.	$\operatorname{Si}_{n}\operatorname{H}_{2n+1}^{-} + \operatorname{Si}\operatorname{H}_{4} \to \operatorname{Si}_{n+1}\operatorname{H}_{2n+3}^{-} + \operatorname{H}_{2}^{-}$	$\sim 10^{-16}$	Langevin $\times 0.1$	n=1,,11	[33]			
Clus	Cluster growth through silylene anions (Si _n H_{2n}^-) with silane							
11.	$\mathrm{Si}_{n}\mathrm{H}_{2n}^{-} + \mathrm{Si}\mathrm{H}_{4} \rightarrow \mathrm{Si}_{n+1}\mathrm{H}_{2n+2}^{-} + \mathrm{H}_{2}$	$\sim 10^{-16}$	Langevin $\times 0.1$	n = 1,, 11	[33]			
Neu	Neutralization reactions of silvl anions with SiH ₂ ⁺ and Si ₂ H ₄ ⁺							
12.	$\operatorname{Si}_{n}\operatorname{H}_{2n+1}^{-} + \operatorname{Si}\operatorname{H}_{3}^{+} \to \operatorname{Si}_{n}\operatorname{H}_{2n+1}^{-} + \operatorname{Si}\operatorname{H}_{3}^{-}$	$\sim 10^{-14}$	calc.	n=1,,12	[39]			
13.	$\operatorname{Si}_{n}\operatorname{H}_{2n+1}^{2n+1} + \operatorname{Si}_{2}\operatorname{H}_{4}^{+} \to \operatorname{Si}_{n}\operatorname{H}_{2n+1} + 2\operatorname{Si}\operatorname{H}_{2}$	$\sim 10^{-14}$	calc.	n=1,,12	[39]			
Neu	Neutralization reactions of silvlene anions with SiH_{a}^{+} and $Si_{2}H_{a}^{+}$							
14.	$Si_nH_0^- + SiH_0^+ \rightarrow Si_nH_{2n} + SiH_3$	$\sim 10^{-14}$	calc.	n = 1,, 12	[39]			
15.	$\operatorname{Si}_{n}\operatorname{H}_{2}^{2n}$ + $\operatorname{Si}_{2}\operatorname{H}_{+}^{+}$ \rightarrow $\operatorname{Si}_{n}\operatorname{H}_{2n}$ + 2 SiH ₂	$\sim 10^{-14}$	calc.	n = 112	[39]			
	2n $2n$ $2n$ $2n$ $2n$ $2n$				r			

 TABLE
 III

 CHEMICAL REACTIONS TAKEN INTO ACCOUNT IN THE MODEL

Indeed, the cross sections for the production of SiH⁻ are too low [26], and SiH- is therefore not considered as a separate species. The partial cross sections of SiH_3^- and SiH_2^- are obtained from [26]. These cross sections are two orders of magnitude smaller than the corresponding dissociative ionization cross sections, but this process represents the most important source of negative ions in the silane plasma. Dissociative attachment cross sections of Si₂H₆ and H₂ can be found in [30] and [31], respectively. However, since the density of Si_2H_6 is more than one order of magnitude lower than the density of SiH₄ (see below), the dissociative attachment to Si_2H_6 is neglected. Although, the rate of electron attachment increases strongly with particle size [32], no electron attachment to larger silicon hydrides is included, since the much lower densities of larger silicon hydrides in comparison to silane makes these attachments less important. Moreover, for particles smaller than 2 nm, the time needed for an electron to attach is much longer than the residence time of the particle in the plasma [32], so there is no possibility for these particles to become charged. H⁻ is not included either, because it appears to have a negligible influence on the plasma chemistry [14].

Table III summarizes the chemical reactions (neutral-neutral reactions and ion-neutral reactions) which are included in our model. The reaction rate coefficients are assumed to be constant. Because some rates are a function of gas temperature or background pressure, their general notation is also given (see the comment column of the table). The values used in our model are calculated for a gas pressure of 0.3 torr or 40 Pa (p_0 is denoted

in Pascal units in Table III) and a gas temperature of 400 K. We consider reactions between silicon hydrides containing up to 12 silicon atoms. An extensive overview is given by Bhandarkar *et al.* [33] and has been utilized to investigate which reactions can be considered as important. The rate constants for larger silicon hydrides in the model of Bhandarkar are based on the calculations made by Girshick and coworkers [33], [34]. Based on the known reactivity and thermochemistry of smaller silicon hydrides, they estimated the thermochemistry and kinetics of larger silicon species. By using a group additivity scheme, the thermodynamic properties of arbitrary silicon hydride clusters could be approximated [34], [35].

The reactions can be subdivided into: 1) H abstraction (reactions 1–4 in Table III); 2) SiH₂ insertion leading to the formation of larger silanes (reactions 5–7); 3) other neutral-neutral reactions (reactions 8–9); 4) anion-neutral (reactions 10–11); and 5) mutual neutralization reactions (reactions 12–15).

1) Reactions Involving Neutrals: A basic set of reactions used to describe a "regular" silane/hydrogen discharge (i.e., without dust formation) has been taken from Nienhuis *et* al. [14] (reactions 1–9, Table III). The rate coefficients of SiH₂ + Si_nH_{2n+2} \rightarrow Si_{n+1}H_{2n+4}, $n \geq 3$ are assumed to be equal to that of SiH₂ + Si₂H₆ \rightarrow Si₃H₈ [14]. Chemical reactions of positive ions with background neutrals, e.g., H₂⁺+SiH₄ \rightarrow SiH₃⁺+H₂+H or SiH₂⁺+SiH₄ \rightarrow SiH₃⁺+SiH₃, have not been included, since they have no influence on the further growth of the clusters. Furthermore, in [14] it is stated that, although the rate coefficients of these reactions are of

equal magnitude as some radical-neutral reactions, the densities of the ions are much lower than the radical densities (see below), making ion-neutral reactions of negligible influence on the densities of the background gases (i.e., SiH₄, Si₂H₆, and H₂). Also, the addition between two radicals to form a higher silane is limited to $Si_2H_5 + Si_2H_5 \rightarrow Si_4H_{10}$. Furthermore, $SiH_3 + SiH_3$ can lead to either Si_2H_6 or $SiH_2 + SiH_4$. However, only the latter reaction is included, since Si₂H₆ is likely to dissociate in SiH₂ and SiH₄ [36]. For completeness, we have also explored other possible reactions between two silyl radicals using the same rate constant as in reactions 8-9 of Table III (i.e., $1.5 \times 10^{-16} \text{ m}^3 \cdot \text{s}^{-1}$). This included reactions such as $Si_3H_7 + SiH_3 \rightarrow Si_4H_{10}$. Adding such reactions to the mechanism generally had no effect on the growth of the species, since our calculations showed that the densities of higher silane radicals are too low to make these reactions effective.

Chemically activated channels for disilane and trisilane decomposition are not incorporated, e.g.,

$$SiH_{2} + SiH_{4} \rightarrow Si_{2}H_{6}^{*} \rightarrow Si_{2}H_{4} + H_{2}$$

$$k = 7.8 \times 10^{-20} \text{ m}^{3} \cdot \text{s}^{-1} \quad (1)$$

$$SiH_{2} + Si_{2}H_{6} \rightarrow Si_{3}H_{8}^{*} \rightarrow Si_{2}H_{4} + SiH_{4}$$

$$k = 1.9 \times 10^{-19} \text{ m}^{3} \cdot \text{s}^{-1} \quad (2)$$

mainly because they do not have an effect on the further cluster growth. Although the above reactions yield a rise in the density of Si_2H_4 , we do not take them into account. Indeed, as stated above, the silylenes are only incorporated in our model because their anions are considered to be important, and they form the neutral silylenes by neutralization reactions (see below).

2) Reactions Involving Anions: Anions are formed by the attachment of electrons to SiH_4 creating SiH_3^- and SiH_2^- . Starting from either SiH_3^- or SiH_2^- , two separate reaction chains lead to the formation of larger negative clusters by anion-neutral reactions. The SiH_3^- ion has a filled valence shell and can slowly cluster with silane

$$\mathrm{SiH}_3^- + \mathrm{SiH}_4 \to \mathrm{Si}_2\mathrm{H}_5^- + \mathrm{H}_2 \tag{3}$$

$$Si_2H_5^- + SiH_4 \rightarrow Si_3H_7^- + H_2 \tag{4}$$

$$Si_nH_{2n+1}^- + SiH_4 \to Si_{n+1}H_{2n+3}^- + H_2$$
 (5)

forming larger silyl anions.

A second important chain of anion-neutral reactions starts from SiH_2^-

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$$\mathrm{SiH}_2^- + \mathrm{SiH}_4 \to \mathrm{Si}_2\mathrm{H}_4^- + \mathrm{H}_2 \tag{6}$$

$$\mathrm{Si}_{2}\mathrm{H}_{4}^{-} + \mathrm{Si}\mathrm{H}_{4} \rightarrow \mathrm{Si}_{3}\mathrm{H}_{6}^{-} + \mathrm{H}_{2} \tag{7}$$

$$\operatorname{Si}_{n}\operatorname{H}_{2n}^{-} + \operatorname{Si}\operatorname{H}_{4} \to \operatorname{Si}_{n+1}\operatorname{H}_{2n+2}^{-} + \operatorname{H}_{2}$$

$$\tag{8}$$

leading to larger silylene anions.

Exact data for the rate constants of these anion-neutral reactions are not known. A theoretical upper limit for anion-molecule collision rates is given by the Langevin rate constants. Since Langevin rates are known to overestimate the actual rates, they are reduced according to [33] by an order of magnitude. The following formula is used to calculate the Langevin rate constants k_L [36]:

$$k_L = e \left(\frac{\pi}{\epsilon_0}\right)^{1/2} \left(\frac{\alpha}{m_r}\right)^{1/2} \tag{9}$$

where α represents the polarizability of the neutral atom or molecule (in Å³) and m_r is the reduced mass (in amu) of the two reacting species. For higher order silicon molecules, a scaling law is used to obtain their polarizability [36]

$$\alpha(\mathrm{Si}_{n}\mathrm{H}_{2n+1}) \approx \alpha(\mathrm{SiH}_{4})[1 + 0.8(n-1)]$$

= 4.62(0.2 + 0.8n) (Å³) (10)

where 4.62 (Å³) represents the polarizability of SiH₄. Hence, the polarizability essentially scales with the number of silicon atoms present in the molecule.

The anion-neutral reactions proceed all at nearly the same reaction rate (about 10^{-16} m³ · s⁻¹, as depicted in Table III). More specifically, the rate slightly decreases from $\begin{array}{l} 1.3 \times 10^{-16} \text{ m}^3 \cdot \text{s}^{-1} \text{ for } \text{SiH}_m^- + \text{SiH}_4^- \rightarrow \text{Si}_2\text{H}_{m+2}^- + \text{H}_2 \\ (m = 2 \text{ or } 3) \text{ to } 9.3 \times 10^{-17} \text{ m}^3 \cdot \text{s}^{-1}, \text{ for } \text{Si}_{11}\text{H}_m^- + \text{SiH}_4 \rightarrow \end{array}$ $Si_{12}H_{m+2}^- + H_2$ (m = 22 or 23). Although in [33] two kinetic bottlenecks in the anion-radical clustering chain are incorporated, we do not take them into account. Indeed, Bhandarkar et al. assumed that the reactions $Si_4H_9^- + SiH_4 \rightarrow Si_5H_{11}^- + H_2$ and $Si_7H^{-}_{15}$ + SiH_4 $\,\rightarrow\,$ $Si_8H^{-}_{17}$ + H_2 are energetically unfavorable, because they lead to a positive change in Gibbs free energy (ΔG) of respectively 7 kcal mol⁻¹ and 9.4 kcal mol^{-1} , whereas the other reactions in the same chain lead to a negative change in the Gibbs free energy [23]. However, since the calculation of the equilibrium constant depends on the thermochemical properties of the reactants and products, which are based on estimations, these bottlenecks might be artificial [40]. Moreover, vibrationally excited silanes may play an important role in the clustering process; hence, these bottlenecks will be eliminated due to the reaction with molecules carrying sufficient internal energy.

Similar to the anion-silane reactions described above, anions can also react with larger silicon hydrides (Si_nH_{2n+2} with n >1), e.g., SiH₃⁻ + Si₂H₆ \rightarrow Si₃H₇⁻ + H₂ or SiH₂⁻ + Si₃H₈ \rightarrow Si₄H₈⁻ + H₂. However, these reactions are not taken into account, because they are nearly two orders of magnitude slower than the chains mentioned above, due to the lower concentrations of Si₂H₆ and especially of the higher order silanes.

In a later stage, we will include the effect of gas temperature on the cluster growth, since it has been experimentally observed that a temperature increase delays the dust formation induction period [32], [41].

It is worth mentioning that even modest production rates of anions can lead to substantial anion densities, because the ambipolar sheath field prevents them from reaching the reactor walls. The loss processes for silyl and silylene anions must therefore occur in the gas phase.

The most important loss process that must be considered is the mutual ion-ion neutralization,

$$\operatorname{SiH}_{3}^{+} + \operatorname{Si}_{n}\operatorname{H}_{m}^{-} \to \operatorname{SiH}_{3} + \operatorname{Si}_{n}\operatorname{H}_{m}$$
(11)



Fig. 1. Density profiles of the ions and electrons at a pressure of 0.3 torr, 5 W, 50 MHz, and 20 sccm inlet silane.

and

$$\operatorname{Si}_{2}\operatorname{H}_{4}^{+} + \operatorname{Si}_{n}\operatorname{H}_{m}^{-} \to 2\operatorname{Si}\operatorname{H}_{2} + \operatorname{Si}_{n}\operatorname{H}_{m}$$
(12)

where m = 2n + 1 for silyl anions (reactions 12–13, Table III) and m = 2n for silylene anions (reactions 14–15 in Table III), respectively. Neutralization of the silyl and silylene anions occurs mainly through reaction with SiH₃⁺, but reactions with Si₂H₄⁺ are not completely negligible. Although another positive ion, H₂⁺, is taken into account in the model, our calculations show that its density is too low to take any significant part in the neutralization process. The rate constants for mutual neutralization between cation *i* and anion *j* are calculated from the semiempirical formula derived by Hickman for gaseous cluster ions [39]

$$k_N \approx 5.34 \times 10^{-13} \times \left(\frac{T_{\text{gas}}}{300}\right)^{-0.5} \times m_r^{-0.5} \times \text{EA}_j^{-0.4} (\text{m}^3 \cdot \text{s}^{-1})$$
 (13)

with the gas temperature T_{gas} in kelvin, the reduced mass m_r in amu, and the electron affinity EA_j in electronvolts (eV). The corresponding electron affinities are taken from [33].

Alternatively, the reactants can also recombine to a larger neutral cluster

$$\operatorname{SiH}_{3}^{+} + \operatorname{Si}_{n}\operatorname{H}_{m}^{-} \to \operatorname{Si}_{n+1}\operatorname{H}_{m+3}.$$
 (14)

However, our calculations show that assuming either neutralization or recombination with the same reaction rate coefficients does not make any difference for the plasma chemistry and the cluster growth. Therefore, we have adopted mutual neutralization instead of recombination, because it requires the introduction of fewer species in the model.

Electron detachment of the negative ions could be another loss process for the negative ions, but it is considered to be negligible in the present study. Furthermore, charge exchange between anions and silyl radicals, e.g., $Si_nH_m^- + Si_nH_{2n+1} \rightarrow$ $Si_nH_m + Si_nH_{2n+1}^-$, has been neglected, since the densities of the various radicals are too low, even if these reactions are also calculated using the Langevin rate constants.

III. RESULTS AND DISCUSSION

The calculations were carried out for a parallel-plate, capacitively coupled RF discharge, for a total pressure of 0.3 torr and a silane gas flow of 20 sccm. The electrode gap is set at 3 cm. Other plasma process parameters include a driving frequency of 50 MHz, a power of 5 W, and a gas temperature of 400 K. These are typical conditions for which cluster formation takes place. The time step is set at 2.5×10^{-10} s and a uniform simulation grid is used.

Typical results of this model are the density profiles and fluxes of the various species, as well as the distribution of the electric field and potential. In this paper, we focus our attention on the densities as a function of distance from the electrodes, which can give us an insight in the clustering process, e.g., which kind of anions are the most important.

The calculated density profiles for the different species listed in Table I are shown in Figs. 1–3 at 0.3 torr, 5 W, 50 MHz, and 20 sccm SiH₄. The electron density is plotted together with the ions in Fig. 1. To emphasize their different behavior, the neutrals, radicals, and ions have been plotted in separate figures.

In Fig. 1, the calculated densities of the ions are shown. A slight time variation of the ion profile will occur in the plasma sheaths; therefore, time-averaged densities of the ions are plotted. The positive ions are represented by a dashed line. The simulation results show that the dominant positive ion is SiH_3^+ with a density of 2×10^{16} m⁻³ in the plasma bulk, which is two times more than the density of $Si_2H_4^+$. Both species densities exceed the density of H_2^+ by almost two orders of magnitude. Therefore, ion-ion recombination reactions with H_2^+ do not have to be included in the model (see above).

All negative ions are confined to the bulk of the plasma and are almost absent in the sheaths. Silyl and silylene anions from n = 3 to n = 11, where *n* represents the number of silicon atoms, reach approximately equal concentrations, especially in the plasma center, and are indicated by the notation $Si_nH_{2n+1}^-$ and $Si_nH_{2n}^-$, respectively. The density profiles of the anions in both pathways appear to slightly increase with increasing *n*. This can be explained by the fact that in our model assumption we have used reduced Langevin rate constants for the anion-neutral reactions, which gradually decreases for larger anions due to an increase of the reduced mass [see (9)], leading to a slower reduction of the anion density. Moreover, for higher order anions, the anion-cation neutralization loss process diminishes, as the reaction rate also gradually decreases with increasing *n* [see (13)].

The two main anion clustering pathways are based on silyl and silylene anions. Therefore, the most prominent species



Fig. 2. Density profiles of silicon hydride molecules at a pressure of 0.3 torr, 5 W, 50 MHz, and 20 sccm inlet silane.

formed are Si₁₂H₂₅⁻ and Si₁₂H₂₄⁻. Indeed, these anions, in the figure also denoted as dust, have a density about two orders of magnitude higher than the other anions, because they are not lost due to the formation of bigger anions. Only the neutralization reactions with SiH₃⁺ and Si₂H₄⁺ provide a possible loss. These two species can thus be considered as the sum of all bigger negative ions. This also implies that $n_{\text{SiH}_3^+} + n_{\text{Si}_2\text{H}_4^+} \cong n_{e^-} + n_{\text{Si}_{12}\text{H}_{25}^-} + n_{\text{Si}_{12}\text{H}_{24}^-}$, where *n* denotes the number densities in the bulk plasma. The electron density is found to be in the order of $5 \times 10^{14} \text{ m}^{-3}$.

The density profiles of the silyl and silylene anions exhibit peaks close to the sheath boundaries. This decrease in density in the plasma bulk is probably due to the fast anion-cation neutralization, which will mainly occur in the center of the discharge, where the density profiles of the positive ions reach a local maximum. As *n* increases, the peaks of the silyl and silylene density profiles tend to shift more inwards, possibly due to the reduced neutralization reaction rate and anion-neutral reaction rate, as explained above. Hence, the Si₁₂H₂₅ and Si₁₂H₂₄ density profiles do not reveal this specific shape, since they represent the sum of the density profiles of all bigger anions, which exhibit a maximum more and more to the center of the discharge.

It is clear from Fig. 1 that the silyl anion pathway (starting from SiH₃⁻) is much more important in comparison with the silylene anion pathway. Indeed, the densities of silyl anions (Si_nH_{2n+1}) are one order of magnitude higher than those of silylene anions (Si_nH_{2n}) , meaning that about 90% of the dust formation proceeds through the silyl anion pathway and only 10% through the silylene anion pathway.

In Fig. 2, the densities of the most important molecules (SiH₄, H₂, and Si_nH_{2n+2} with n > 1) are represented. The densities of the molecules are homogeneously distributed throughout the entire reactor and these species have much higher densities



Fig. 3. Density profiles of the various silicon hydride radicals at a pressure of 0.3 torr, 5 W, 50 MHz, and 20 sccm inlet silane.

than the radicals, e.g., SiH₃ (see Fig. 3), which do undergo reactions at the electrodes. The densities of SiH_4 , H_2 , and Si_2H_6 are at least one order of magnitude higher than other neutral molecules and are commonly referred to as background neutrals. The inlet gas SiH₄ is present at the highest density (about 4×10^{21} m⁻³), but also H₂ has a rather high density of almost 3×10^{21} m⁻³. This is due to the fact that in many of the chemical reactions shown in Table III, molecular hydrogen is formed as a side product (e.g., reactions 1, 2, 4, 10, and 11). The higher order silanes, especially Si₂H₆, can, however, not be neglected either. Finally, note that, similar to Fig. 1, the density of the largest neutral species, $Si_{12}H_{26}$, is higher than would have been expected from the trend in decreasing density for higher molecules. This is due to the SiH₂ insertion reactions, which are stopped at Si₁₂H₂₆. Hence, again, Si₁₂H₂₆ stands for all higher order silanes.

In Fig. 3, the density profiles of the various radical species are shown. The radicals show a decreasing density toward the electrodes, representing their reactivity at the surface. The Si_nH_{2n+1} radicals (with n = 1 to 12), related to the silyl anions, are represented with a solid line, so that they are distinguished from the silvlenes (Si_nH_{2n}, with n = 1 to 12), represented by a dashed line. The most important radical in the silane discharge is SiH₃ with a density of about $3 \times 10^{18} \text{ m}^{-3}$ in the center of the discharge. Again, the densities of Si₁₂H₂₅ and Si₁₂H₂₄ stand for a summation of the densities of all higher radicals. For reasons of clarity, the concentrations of all silvlenes containing two to eleven silicon atoms are represented by a single line, since these species reach approximately the same concentration (due to the fact that the neutralization of silvlene anions proceeds at almost the same reaction rate and it represents their only production process). As can been seen from Fig. 3, the silvlenes have a relatively low density and thus are not considered to be important in our simulations. They

are only included since their respective anions form a possible clustering pathway.

IV. CONCLUSION

In this paper, we have used a one-dimensional fluid model to simulate cluster generation in silane plasmas and we have mainly focused our attention on particle nucleation and further growth. A total of 111 reactions among 65 silicon hydrides containing up to 12 silicon atoms were included in this model. Density profiles for the most important species were presented as a function of distance from the electrodes.

The anions play an indispensable role in the polymerization process, as negative ion-silane reactions represent the main pathway of particle growth. SiH₃⁻, produced by dissociative electron attachment, forms the main starting point of anion formation and can be considered as the most important precursor of the dust formation. SiH₂⁻, although less important, leads to the formation of silylenes anions (Si_nH_{2n}). The silyl anion pathway, starting from SiH₃⁻ and leading to the formation of Si_nH_{2n+1} species, is much more important in comparison with the silylene anion pathway. It follows from our model that about 90% of the dust formation proceeds through the silyl anion pathway and only 10% through the silylene anion pathway.

In the future, this model will form the starting point for nanoparticle formation, and as the particles increase in size, coagulation of the clusters will be added.

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