Plasma-based N_2 *fixation into* NO_x :

Insights from modeling toward optimum yields and energy costs in a gliding arc plasmatron

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Figure S.3 Energy cost for NO_x production as a function of the χ parameter, compared to the reported works from literature and the results of Pei et al. using different plasma sources. The figure is adapted from ref.¹ with the permission from the authors. The χ parameter of our GAP is plotted in pink (for the conditions described in the section below).

7. Reaction analysis _____

Figure S.4 Net rates of the most important formation and loss process of NO (and NO_2) as a function of the N_2 fraction in the feed gas, at the same condition as in Figure 1 in the main paper.

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Figure S.7 Calculated number densities of NO, NO₂, O and N (a), and net rates of the main reactions as function of the residence time (b), for an $80/20 N_2/O_2$ mixture at 1.25 bar, 10 L min⁻¹ and 415 W.

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9. Chemistry set

Table S.8 Electron impact reactions implemented in the model for atomic and molecular nitrogen and oxygen species as well as NO_x species. The list includes vibrational excitation and de-excitation, electronic excitation and de-excitation, direct and dissociative ionization, dissociation, as well as direct and dissociative attachment reactions. These reactions are treated by energy-dependent cross sections when the rate coefficient is not specified. When indicated, rate coefficients are expressed in cm³ s⁻¹ or cm⁶ s⁻¹ for binary or ternary reactions, respectively.

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Table S.11 Ion-neutral reactions included in the model and the corresponding rate coefficient expressions. T_g is the gas temperature in K. For certain reactions, T_{ion} is the effective temperature of the reacting ion in K [26]. The rate coefficients are expressed in cm³ s⁻¹ or cm⁶ s⁻¹ for binary or ternary reactions, respectively.

Table S.12 Ion-ion reactions included in the model, the corresponding rate coefficient expressions and the references. T_g is the gas temperature in K. The rate coefficients are expressed in cm³ s⁻¹ or cm⁶ s⁻¹ for binary or ternary reactions, respectively.

Table S.13 Optical transitions of N_2 and O_2 species. The rate coefficients are expressed in s^{-1} .

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1. Comparison with different plasma sources applied for NO_x formation

Table S.1 Yield and energy cost for NO_x formation in different plasma sources. They all operate at atmospheric pressure, unless mentioned otherwise. The HB process for NH_3 synthesis is also added, as benchmark.

Reactor	Yield [%]	Energy cost [MJ/mol]	Ref.
GAP	1.5 % NO _x	3.6 MJ/mol NO _x	This work
Electric arc (Birkeland – Eyde)	1 – 2 % NO	2.41 MJ/mol NO	2
Electric arc with water injection	2.41 % NO	3.5 MJ/mol NO	3
MW at reduced pressure with MoO ₃ catalyst	6 % NO	0.84 MJ/mol NO	4
Pulsed MW at reduced pressure	6 % NO	0.60 MJ/mol NO	5
MW with magnetic field at reduced pressure	14 % NO	0.30 MJ/mol NO	6
DBD with $\gamma - Al_2O_3$ catalyst	0.5 % NO _x	18 MJ/mol NO _x	7
Shielded sliding discharge	0.1 % NO _x	15.4 MJ/mol NO _x	8
Pulsed milliscale GA	2 % NO _x	2.8 MJ/mol NO _x	9
Haber – Bosch	$10-20 \% \ NH_3{}^a$	0.48 MJ/mol ^a	10

a. Yield after one pass, depending on the specific plant, and energy cost of the whole process.

2. Details on the experimental setup



Figure S.1 Schematics of the entire experimental system used for the experimental procedure that was explained in the main paper.

For safety and environmental concerns, we have NO and NO_2 sensors in the lab to detect any probable leak. In addition, the whole experimental setup is placed in a separated fume hood, connected to special air filters to avoid introducing the exhaust gas to the open air and harming the environment.

3. **0D model description**

A zero-dimensional (0D) chemical kinetics model was developed to solve a set of continuity equations (Eq. 2) for all individual species included in the model (see Table S.2), in order to obtain the species densities as a function of time:

$$\frac{\mathrm{d}n_{i}}{\mathrm{d}t} = \sum_{j} \left[\left(a_{ij}^{\mathrm{R}} - a_{ij}^{\mathrm{L}} \right) k_{j} \prod_{l} n_{l}^{\mathrm{L}} \right]$$
(2)

 n_i is the density of species i, a_{ij}^R and a_{ij}^L are the right and left stoichiometric coefficients for the following general reaction:

$$aA + bB (+\Delta H) \xrightarrow{k_j} cC + dD (+\Delta H)$$
 (3)

With species *i* for reaction *j*. Here, *A*, B, *C* and *D* are the different species and *a*, *b*, *c* and *d* are their respective stoichiometric coefficients. ΔH represents the enthalpy of reaction *j*. The reaction rate coefficient, k_j , of the heavy particle reactions are either constant or dependent on the gas temperature and are expressed in cm³ s⁻¹ or cm⁶ s⁻¹ for two-body or three-body reactions, respectively. The rate coefficients of the electron impact reactions can depend on the electron temperature T_e (or the reduced electric field E/N, i.e., the electric field E divided by the number density of all neutral species N, usually expressed in Td = $10^{-21} \frac{V}{m^2}$). Most rate coefficients of electron impact reactions are calculated according to the following equation:

$$k_{i} = \int_{\varepsilon_{th}}^{\infty} \sigma_{i}(\varepsilon) v(\varepsilon) f(\varepsilon) d\varepsilon$$
(4)

 ε is the electron energy (usually in eV), ε_{th} is the minimum threshold energy needed to induce the reaction, $v(\varepsilon)$ the velocity of the electrons, $\sigma_i(\varepsilon)$ is the cross section of collision *i*, and $f(\varepsilon)$ is the electron energy distribution function (EEDF). We use the ZDPlasKin¹¹ code to solve the balance equations (Eq. 2) for all species, which has a built-in Boltzmann solver, BOLSIG+¹², to calculate the EEDF and the rate coefficients of the electron impact reactions based on a set of cross sections, the plasma composition, the gas temperature and the reduced electric field (E/N). The electric field (E) is calculated from a given power density, using the so-called local field approximation¹³:

$$E = \sqrt{\frac{P}{\sigma}}$$
(5)

P is the input power density (W m⁻³) and σ is the plasma conductivity (A V⁻¹ m⁻¹). The plasma conductivity is¹³

$$\sigma = e n_e \mu_e \tag{6}$$

 n_e is the electron number density and μ_e is the electron mobility.

The model is applied to the GAP reactor at exactly the same dimensions and operating conditions as in the experiments. A schematic diagram of the GAP, including the dimensions, is presented in Figure S.2. The arc plasma column inside the GAP is illustrated by the red rectangle. Because the gas enters the GAP reactor by tangential inlets, it follows a vortex flow pattern. As the outlet (anode) diameter is smaller than the reactor body (cathode part) (see Figure S.2a), the gas will first move upwards in a so-called forward vortex flow (indicated in Figure S.2a by the solid spiral). When the gas arrives at the top of the reactor, it will have lost most of its speed by friction and inertia. The gas will then travel downwards in a smaller so-called reverse vortex flow, which is more or less captured by the arc column (see dashed spiral in Figure S.2a).

The reverse vortex flow results in the stabilization of the arc column in the centre of the GAP, as was previously predicted by 3D fluid dynamics simulations.^{14,15} The vast majority of the plasma conversion thus takes place in the column-shaped centre of the reactor. Since the plasma is confined

in the inner vortex of the gas flow, the plasma can be considered uniform and we can assume a constant power density applied to the gas during its residence time in the plasma. This is convenient for the 0D model, which does not include spatial variations or transport. However, the calculated temporal dependence of the species densities can be transformed into a spatial dependence through the reactor by means of the gas flow rate^{16,17} (see Figure S.2b). The arc plasma column is thus considered as a plug flow reactor, where the plasma characteristics vary as a function of distance travelled by the gas within a certain residence time, in the same way as they would vary as a function of time in a batch reactor. 2D fluid dynamics simulation results of Trenchev et al. for a GAP in argon ^{14,15} revealed that the arc radius is typically around 1 mm. However, the temperature just outside this arc region is still high enough to induce plasma, especially in a molecular plasma where vibration-translation (VT) relaxation causes gas heating. Therefore, we assumed an arc radius of 2 mm in our simulations. Combined with the length of the cathode (10.20 mm) and anode (16.30 mm) and the inlet of 3 mm (see Figure S.1), this yields a plasma volume of 0.37 cm³. These input data were also successfully used in ^{18–20}.



Figure S.2 (a) Schematic illustration of the GAP, indicating its dimensions as well as the outer vortex (solid spiral) and the inner (reverse) vortex (dashed spiral). The red frame indicates the plasma arc column, while the blue part indicates the region where the gas leaves the reactor without being treated. (b) Schematic of the 0D modeling approach in which the time dependency is translated into a spatial dependency by means of the gas flow rate.

We assume a constant temperature of 3000 K as input in our model, based on 3D fluid dynamics simulations^{14,15}. Note that the calculated value was obtained for CO₂, and the experimental value for pure N₂, but not for N₂/O₂ gas mixtures. We expect the temperature profiles to be similar as they are all molecular gasses, as they experience the same mechanisms causing gas heating. We can also safely assume that the gas is already heated up to 3000 K when it enters the inner vortex, where the majority of the conversion takes place, so this is why the temperature profile starts at 3000 K and is kept constant. Gröger et al. have measured a gas temperature of 5000 K in our GAP operating in pure N₂.²¹ This high temperature, however, likely originates from the hot cathode spot, so we think that 3000 K is a better estimate of the gas temperature inside the arc.

As initial conditions in the plasma, we start with a fixed electron density of 10^{10} cm⁻³, considering only N₂ and O₂ molecules, including their vibrationally excited equivalents, N₂⁺ and O₂⁺ ions and electrons. We assume quasi-neutrality by setting the electron density equal to the sum of the densities of the N₂⁺ and O₂⁺ ions, according to their fraction in the inlet mixture. In addition, we assume a Boltzmann distribution for all vibrationally exited species, at a temperature of 3000 K. The sum of the initial densities of N₂, N₂(v_x) and N₂⁺ ions amounts to the total density that N₂ would have according to its initial fraction in the feed. Similarly, the sum of the initial densities of O₂, O₂(v_x) and O₂⁺ ions is according to the O₂ fraction in the feed.

Vibrational excitation of N₂ is promoted in the GAP and is advantageous for more energy-efficient dissociation of N₂, because it can help to overcome the reaction energy barrier of the Zeldovich mechanism.^{22,23} Therefore, special attention is given to the vibrational levels: 24 vibrational levels for N₂ and 15 levels for O₂ were implemented in the model. The species taken into account in the model are listed in Table S.2. This includes neutral molecules in the ground, vibrationally and electronically excited states, various radicals, positive and negative ions, and electrons. In total, 1195 different electron impact, 435 neutral-neutral, 523 ion-neutral and 48 ion-ion chemical reactions are included, as well as 2478 vibrational-vibrational (VV) exchanges and vibrational-translational (VT) relaxations between N₂ – N₂, O₂ – O₂, and N₂ – O₂, and between O₂ – O₂, N₂ – N₂, N₂ – N and O₂ – O, for all vibrational levels. The reaction set of in reference ²⁴ was revised and used, but with the addition of N₂ – O₂ VV exchanges and N₂ – N and O₂ – O VT relaxations. The latter processes do not significantly influence the NO_x formation at the conditions under study, but were included for the sake of completeness. The N₂ – O₂ VV exchanges are demonstrated to be very important (cf. Figure 6 in the main paper). The vibrational levels of NO and NO₂ are not included, because of lack of data on their vibrational kinetics in literature. All reactions are listed under section 9.

N ₂ species				
Neutral ground state molecules	<i>N</i> ₂			
Ions	N^+ , N_2^+ , N_3^+ , N_4^+			
Vibrationally excited molecules	$N_2(v_1 - v_{24})$			
Electronically excited molecules or atoms	N ₂ (A ³ Σ_{u}^{+}), N ₂ (B ³ Π_{g}), N ₂ (C ³ Π_{u}) and N ₂ (a ^{'1} Σ_{u}^{-}), N(2D), N(2P)			
Radicals	Ν			
N _x O _y species				
$NO, N_2O, NO_2, NO_3, N_2O_5, N_2O_3, N_2O_4, NO^+, N_2O^+, NO_2^+, NO^-, N_2O^-, NO_2^-, NO_3^-, O_2^+N_2O_3^-, NO_2^-, NO_3^-, NO_$				
O ₂ species				

Table S.2 Species included in the model

Neutral ground state molecules	<i>0</i> ₂ , <i>0</i> ₃
Ions	$0^-, 0_2^-, 0_3^-, 0_4^-, 0^+, 0_2^+, 0_4^+$
Vibrationally excited molecules	$O_2 (v_1 - v_{15})$
Electronically excited molecules or atoms	$O(1D), O(1S), O_2(a^1\Delta), O_2(b^1\Sigma^+)$ and a combination of three states, i.e. $O_2(A^3\Sigma^+, C^3\Delta, c^1\Sigma^-)$ at a threshold energy of 4.5 eV.
radicals	0

The product yield, also reported in the main paper, is defined as:

$$Y_{x} = Y_{x,arc} \cdot f \tag{7}$$

where f is the fraction of gas passing through the plasma arc and is defined as:

$$f = \frac{Q_{\text{plasma}}}{Q_{\text{inlet}}} \tag{8}$$

where Q_{inlet} is the flow rate at the inlet of the rector and Q_{plasma} is the flow rate of the gas in the plasma region (red frame in Figure S.1(a)). In a GAP operating at atmospheric pressure, only14.8% of the gas flows through the plasma region and the remaining 85.2% is assumed in this model to leave the reactor without being treated. $Y_{x,arc}$ corresponds to the product yield in the plasma arc region and is defined as:

$$Y_{x,arc} = \frac{n_x}{n_0} \cdot 100\% \tag{9}$$

where n_x is the density (cm⁻³) of species x, for example NO or NO₂ and n_0 is the initial gas density.

4. Detailed experimental results

The experimental procedure consists of stabilizing the plasma for 15 minutes, followed by online continuous mass spectrometry measurements, and at the same time recording the plasma voltage and current in order to calculate the plasma power, and finally a cool down and flush period of 30 minutes with the next gas mixture. Each condition is repeated for three times and the results shown below are, thus, the average of these three measurements.

4.1Plasma power measurement

To calculate the plasma power, we measured the voltage and current passing through the arc. For this purpose, an oscilloscope (Tektronix TDS2012C) was used. The voltage was measured using a high voltage probe (Testec) connected to the cathode, the ground wire and channel 1 of the oscilloscope. The current was measured over an external resistor box by a wire connection to the second channel of the oscilloscope, using I = V/R with the resistance of the resistor box being 6 Ohm. The potential and current over a certain period of time were used to calculate the plasma power with the following formula:

$$P_{\text{plasma}} = \frac{1}{T} \int_0^{t=T} V_{\text{plasma}} \cdot I_{\text{plasma}} dt$$
(1)

Also, several pressure sensors were placed along the gas circuit to monitor the correct working of the setup during the experiments. Table S.3 shows the average plasma power measured by the oscilloscope, as well as the specific energy input (SEI) for each N_2/O_2 ratio with a total flow rate of 10 L/min. The error values are also indicated in Table S.3.

N ₂ /O ₂ ratio	Total flow rate [L/min]	Flow rate- error	Average plasma power [W]	Power- error	SEI [J/L]	SEI- error
9/1	10.00	0.07	365	9	2190	57
8/2	10.00	0.07	369	28	2214	171
7/3	10.00	0.07	379	11	2274	69
6/4	10.00	0.07	409	25	2454	151
5/5	10.00	0.07	415	11	2492	71
4/6	10.00	0.07	434	23	2606	139
3/7	10.00	0.07	437	13	2624	83
2/8	10.00	0.07	458	12	2748	75
1/9	10.00	0.07	381	33	2289	201
8/2	8.000	5.01	490	5	3679	48
8/2	12.000	17.84	390	18	1951	90
8/2	14.000	32.08	428	16	1837	70
8/2	16.000	25.56	548	26	2057	97
8/2	18.000	29.70	390	30	1299	99
8/2	20.000	11.12	490	11	1471	34
8/2	22.000	33.85	364	34	993	92
8/2	25.000	11.55	476	12	1144	28
8/2	30.000	12.89	375	13	750	26

Table S.3 Average plasma power for different N_2/O_2 ratios and different flow rates.

4.2Gas analysis and product concentrations

The output gas composition was analyzed online by a mass spectrometer (Hiden Analytical Limited, QGA Pro v1.6). The mass spectrometer was calibrated separately with a mixture of 867 ppm NO₂ in He and 976 ppm NO in He. For both NO and NO₂, a response factor was calculated and used to determine the concentration of the detected products, which is 1696 for NO and 313 for NO₂. Table S.2 shows the NO and NO₂ concentrations (ppm) before calibration, the calibrated concentrations (ppm), as well as the product selectivity for different N₂ and O₂ gas mixtures.

Table S.4 NO and NO₂ concentrations (ppm) before calibration, calibrated concentrations (ppm) and product selectivity. We also checked for N_2O and N_2O_4 but their concentrations were below the detection limit.

N ₂ /O ₂ ratio	NO concentration	Calibrated- NO [ppm]	NO ₂ concentration	Calibrated- NO ₂ (ppm)	NO selectivity	NO ₂ selectivity
	[a.u.]				[%]	[%]
9/1	7.61x10 ⁻⁸	1.29x10 ⁻⁴	1.73x10 ⁻⁸	5.41x10 ⁻⁶	95.97	4.03
8/2	8.04x10 ⁻⁸	1.36x10 ⁻⁴	4.26x10 ⁻⁸	1.33x10 ⁻⁵	91.09	8.91
7/3	7.90x10 ⁻⁸	1.34x10 ⁻⁴	6.04x10 ⁻⁸	1.89x10 ⁻⁵	87.63	12.37
6/4	7.61x10 ⁻⁸	1.29x10 ⁻⁴	8.03x10 ⁻⁸	2.51x10 ⁻⁵	83.70	16.30
5/5	7.24x10 ⁻⁸	1.23×10^{-4}	8.43x10 ⁻⁸	2.64x10 ⁻⁵	82.31	17.69
4/6	6.57x10 ⁻⁸	1.11x10 ⁻⁴	8.17x10 ⁻⁸	2.56x10 ⁻⁵	81.33	18.67
3/7	6.20x10 ⁻⁸	1.05x10 ⁻⁴	7.90x10 ⁻⁸	2.47x10 ⁻⁵	80.96	19.04
2/8	5.45x10 ⁻⁸	9.24x10 ⁻⁵	7.03x10 ⁻⁸	2.20x10 ⁻⁵	80.77	19.23
1/9	4.04x10 ⁻⁸	6.85x10 ⁻⁵	4.52x10 ⁻⁸	1.41x10 ⁻⁵	82.89	17.11

4.3Energy measurements

Table S.5 Measured energy cost (EC) with the corresponding error values for different N_2/O_2 ratios.

N ₂ /O ₂ ratio	EC	EC-error
9/1	3.99×10^{6}	0.10×10^{6}
8/2	3.62×10^6	0.28×10^{6}
7/3	3.64×10^{6}	0.11×10^{6}
6/4	3.90×10^{6}	0.24×10^{6}
5/5	4.09×10^{6}	0.12×10^{6}
4/6	4.66×10^{6}	0.25×10^{6}
3/7	4.95×10^{6}	0.16×10^{6}
2/8	5.88×10^{6}	0.16×10^{6}
1/9	6.78×10^6	0.59×10^{6}

5. Raw data from the model

Table S.6 Calculated yield of NO and NO₂ and energy consumption (EC) as a function of N₂ fraction in the feed gas, for a gas flow rate of 10 L min⁻¹, a pressure of 1.25 bar and a power ranging from 365 to 458 W (slightly varying for different gas composition; see Table S.3).

N ₂ [%]	NO [%]	NO ₂ [%]	EC [MJ/mol]
10	0.48	0.06	11.44
20	0.76	0.08	7.98
30	1.01	0.10	5.77

40	1.30	0.12	4.49	
50	1.44	0.12	3.91	
60	1.49	0.11	3.75	
70	1.44	0.10	3.63	
80	1.35	0.07	3.81	
90	1.11	0.04	4.66	

Table S.7 Calculated density of N_2O , N_2O_4 , NO_3 , N_2O_5 and N_2O_3 as a function of N_2 fraction in the feed gas, for a gas flow rate of 10 L min⁻¹, a pressure of 1.25 bar and a power ranging from 365 to 458 W (slightly varying for different gas compositions; see Table S.3).

N ₂ [%]	N ₂ O [cm ⁻³]	N ₂ O ₄ [cm ⁻³]	NO ₃ [cm ⁻³]	N_2O_5 [cm ⁻³]	N_2O_3 [cm ⁻³]
10	6.81×10^{12}	1.16×10^5	5.22×10^{13}	1.02×10^5	8.62×10^7
20	1.66×10^{13}	2.53×10^5	8.11×10^{13}	2.34×10^5	2.04×10^8
30	2.81×10^{13}	3.76×10^5	9.62×10^{13}	3.39×10^5	3.31×10^8
40	4.58×10^{13}	5.29×10^5	1.10×10^{14}	4.59×10^5	5.05×10^8
50	5.75×10^{13}	5.47×10^5	1.04×10^{14}	4.44×10^5	5.68×10^8
60	6.54×10^{13}	4.86×10^5	9.04×10^{13}	3.62×10^5	5.55x10 ⁸
70	6.58×10^{13}	3.49×10^5	6.78×10^{13}	2.30×10^5	4.55×10^8
80	6.49×10^{13}	2.11×10^5	4.40×10^{13}	1.16×10^5	3.31×10^{8}
90	5.37×10^{13}	6.86×10^4	1.75×10^{13}	2.64×10^4	1.55×10^{8}

6. Benchmarking the energy cost of our GAP reactor: Chi parameter

The various plasma sources listed in Table S.6 are all different in structure, geometry and excitation modes, and they potentially have different chemical reaction pathways for NO_x production. Therefore, Pei et al. proposed a dimensionless parameter (χ) to compare different plasma set-ups ¹.:

$$\chi = \frac{\overline{E} \cdot \overline{T}}{\overline{E}_{r} \cdot \overline{T}_{r}} \tag{4}$$

Where \overline{E} and \overline{T} are the average electric field and average gas temperature of a specific plasma type, and \overline{E}_r and \overline{T}_r are reference values chosen to normalize these parameters at 1.43 kV/cm and 1800 K, respectively.



Figure S.3 Energy cost for NO_x production as a function of the χ parameter, compared to the reported works from literature and the results of Pei et al. using different plasma sources. The figure is adapted from ref.¹ with the permission from the authors. The χ parameter of our GAP is plotted in pink (for the conditions described in the section below).

They observed that the energy cost (reported per unit of reactive N, expressed in units of GJ/tN) increases linearly with χ for different plasma types evaluated, and thus they concluded that χ can give a good indication of the energy cost performance of a specific plasma set-up for NO_x production. Based on the calculated gas number density of 3.02×10^{18} cm⁻³ and an average reduced electric field of 16 Td, we estimate for our GAP an average electric field of 0.48 kV/cm, while the average gas temperature in the arc should be around 3000 K¹⁵. This yields a χ value of 0.56. The minimum energy cost in GJ/tN in our GAP is 257 GJ/tN. If we would add this data point to the figure in ref.²⁵ (see pink square on Figure S.3), our EC is in the range of what is predicted by the linear dependency between EC and χ .

7. Reaction analysis

The net rates for the production or loss of NO and NO₂, discussed in the main paper, are plotted as a function of the N₂ fraction in the feed gas in Figure S.4. As NO₂ is always formed from NO, the main processes for the formation and loss of NO₂ are also included in this figure, though formulated as an NO loss instead of an NO₂ formation process. For the sake of clarity, we have plotted processes N1 and N5 on the right y-axis, which is 10 times larger than the left y-axis, so that the evolution of the rates of the Zeldovich processes (N2 and N3) is clearly visible. The Zeldovich mechanism (N2 and N3) as a function of the N₂ fraction in the feed is discussed in section 3.4 of the main paper. As seen in Figure S.4, N1 is the dominant NO formation reaction at N₂ fractions below 60 %. At higher N₂ fractions, reaction N2 becomes more important, as there is less O₂ available. NO is rapidly converted

into NO₂ through N4 (pink curve in Figure S.4). Its rate drops with increasing N₂ fraction, as this process requires atomic O. Next, NO₂ is converted back to NO through N1 (red curve) and N4 (purple curve), which are the two main loss channels for NO₂.



Figure S.4 Net rates of the most important formation and loss process of NO (and NO₂) as a function of the N_2 fraction in the feed gas, at the same condition as in Figure 1 in the main paper.



Figure S.5 Net rates of the most important formation and loss processes of NO as a function of the O_3 fraction in the feed gas at a N_2/O_2 ratio of 80/20, flow rate of 10 L min⁻¹ and a power of 400 W.



Figure S.6: Calculated number densities of NO, NO₂, O and N (a), and net rates of the main reactions as function of residence time until steady state (b), for an 80/20 N_2/O_2 mixture at 1.25 bar, 10 L min⁻¹ and 415 W. The same figure for the full residence time (15 ms) can be found in Figure S.7. Panel (c) shows reactions N2 and N3 in detail.

The NO, NO₂, N and O densities reach steady state already in the first 0.5 ms, which can be explained as follows. First, the N atoms are predominantly (99.98 %) formed through electron impact dissociation of $N_2(g/v)$ (see peak in Figure S.6a: purple curve). The N atoms are partially consumed in the Zeldovich mechanism (Figure S.6b and c: blue curve, N3) with the formation of NO. Similarly, the O atoms are formed through direct electron impact dissociation and collision with electronically excited N_2 molecules (as discussed of the main paper) and partially consumed through the second step of the Zeldovich mechanism (Figure S.6b and c: black curve, N2). Once NO is formed, it is either (1) converted into NO₂ (Figure S.6b: pink curve, N4), or (2) destroyed through the backward reaction of N2. Indeed, the rate of N2 becomes negative around 0.5 ms (see Figure S.6b and c: black curve). In case it had been converted into NO₂ it is partially converted back into NO (Figure S.6b: red curve, N1). Under these conditions the backward reaction of N3 is not promoted, and the net reaction rate is in favor of NO production throughout the entire residence time. On the other hand, the net rate of N2 is in favor of NO production before 0.5 ms, but decreases after 0.5 ms in favor of NO desctruction. This limits the NO production."



Figure S.7 Calculated number densities of NO, NO₂, O and N (a), and net rates of the main reactions as function of the residence time (b), for an $80/20 N_2/O_2$ mixture at 1.25 bar, 10 L min⁻¹ and 415 W.

8. VDFs of N₂ and O₂

In this section we give a more elaborate description and discussion of the VDF of N_2 an O_2 to support our discussion in the main paper.

The chemistry set we developed for this model includes an extensive description of the vibrational kinetics of both N_2 and O_2 . A simple measure of the degree of vibrational excitation is the vibrational temperature, calculated according to:

$$T_{\nu} = \frac{1}{m} \sum_{1}^{m} - \frac{(E_{i} - E_{i-1})}{\ln(\frac{n_{i}}{n_{i-1}})}$$
(5)

With m being an integer corresponding to the number of vibrational levels taken into account in the calculation of the vibrational temperature, E_i is the vibrational energy of the ith level and n_i is the density of the molecule at the ith level. The vibrational temperature, based on the 24 vibrational levels of N₂ included in the model, is calculated to be 3325 K. This is slightly higher than the gas temperature in the arc, which is expected to be around 3000 K, based on 2D fluid dynamics modeling¹⁵, and taken as constant in our model (see section 4 above). The vibrational temperature of O₂ is calculated to be 2632 K, based on the 15 vibrational levels of O₂ taken into account in the model. Hence, this is somewhat lower than the vibrational temperature of N₂. Indeed, even though the reaction rate



Figure S.8 Normalized vibrational distribution function (VDF) of N_2 (a) and O_2 (b) at different times in the plasma for a 50/50 N_2/O_2 plasma, and at the same conditions as in Figure 1. The solid and dashed curves represent the VDFs of a chemistry set that includes and excludes $N_2 - O_2$ VV exchanges, respectively (see next section). The black full lines (representing t = 1.5 and 2.5 ms) are on top of one another, as well as the black dashed lines, indicating that the VDFs of N_2 and O_2 reach steady state already after 1.5 ms. For comparison, the thermal VDF at 3000 K is also plotted as a dotted blue curve.

constants of $N_2 - N_2$ vibrational ladder climbing (by vibrational-vibrational (VV) exchanges) are five times lower than for $O_2 - O_2$ vibrational ladder climbing, the reaction rate constants of the different depopulation mechanisms of the O_2 vibrational levels (i.e., by vibrational-translational (VT) exchanges: $O_2 - O$ VT, $O_2 - N_2$ VT and $O_2 - O_2$ VT) are higher than the rate constants of the same mechanisms for the N_2 vibrational levels, resulting in easier depopulation of the O_2 vibrational levels. In Figure S.8, we plot the vibrational distribution function (VDF), i.e., normalized density of the vibrational levels, of N_2 (panel a, solid lines) and O_2 (panel b, solid lines), at different times in the

plasma, as well as the thermal distribution of N_2 and O_2 at 3000 K (dotted, light blue curves). The VDF of N_2 is in thermal equilibrium for the majority of the residence time. At short residence time (t = 0.01 ms), the vibrational temperature is much lower than 3000 K, but the population quickly builds up, to a vibrational temperature above 3000 K at 1.5 ms. The VDF of O_2 shows an overpopulation of the higher vibrational levels at short residence times (t = 0.01 ms), but after 1.5 ms, the VDF also becomes in equilibrium, with a temperature slightly below the gas temperature of 3000 K. Both VDFs reach a quasi-steady state after 1.5 ms. Although the VDFs are thermal, the higher vibrational levels are nevertheless sufficiently populated to facilitate dissociation, as illustrated in Figure 3 and Table 1 in the main paper. Moreover, the vibrational levels in our GAP are more populated than in other set-ups, like a classical GA, where the VDF drops significantly for the higher vibrational levels.²⁴

9. Chemistry set

The chemistry set used in this model is based on the work done by Wang et al.²⁴, but revised and updated. For instance, the set contains a more elaborate description of the vibrational kinetics of N₂ and O₂ (i.e. N₂ – O₂ vibrational-vibrational (VV) exchanges and N₂ – N and O₂ – O vibrational-translational (VT) relaxations, see Table S.13). 24 vibrational levels for N₂ and 15 levels for O₂ were implemented in the model. The species taken into account in the model are listed in Table S.5 above. This includes neutral molecules in the ground state, vibrationally and electronically excited states, various radicals, positive and negative ions, and electrons. Table S.7 lists all electron impact reactions. Most of these reactions are treated by energy-dependent cross sections. Table S.8 lists the neutral-neutral reactions and the corresponding rate-coefficient expressions. For certain reactions, the rate coefficients of the vibration energy is lowered by αE_v , where α is the vibrational efficiency to lower the activation barrier and E_v is the vibrational energy. For those reactions, the α parameter is given in the last column of Table S.8. Tables S.9 to S.11 list the electron-ion recombination, the ion-neutral and the ion-ion reactions and the corresponding rate coefficients, respectively. Table S.12 displays the optical transitions

Table S.8 Electron impact reactions implemented in the model for atomic and molecular nitrogen and oxygen species as well as NO_x species. The list includes vibrational excitation and deexcitation, electronic excitation and de-excitation, direct and dissociative ionization, dissociation, as well as direct and dissociative attachment reactions. These reactions are treated by energydependent cross sections when the rate coefficient is not specified. When indicated, rate coefficients are expressed in $cm^3 s^{-1}$ or $cm^6 s^{-1}$ for binary or ternary reactions, respectively.

Reaction	Rate Coefficient	Ref.	Note
$e^- + N_2 \leftrightarrow e^- + N_2(v)$		26	
$e^- + N_2(v) \leftrightarrow e^- + N_2(v')$		26	
$e^{-} + N_2(g, v) \rightarrow e^{-} + N_2(E_x)$		27	a, b, c
$e^- + N_2(E_x) \rightarrow e^- + N_2$		27	b
$e^- + N_2(g, v) \rightarrow 2e^- + N_2^+$		28	а
$e^- + N_2(E_x) \rightarrow 2e^- + N_2^+$		28	b
$e^- + N \rightarrow 2e^- + N^+$		27	
$e^- + N_2(g, v) \rightarrow 2e^- + N^+ + N$		29	а
$e^- + N_2(g, v) \rightarrow e^- + N + N$		27	a, c
$e^- + N_2(E_x) \rightarrow e^- + N + N$		27	b
$e^- + N \rightarrow e^- + N(E_x)$		27	d
$e^- + 0_2 \leftrightarrow e^- + 0_2(v)$		26	
$e^- + O_2(v) \leftrightarrow e^- + O_2(v')$		30	

$e^- + O_2(g, v) \rightarrow e^- + O_2(E_x)$		27	a, c, e
$e^- + O_2(E_x) \to e^- + O_2$		27	e
$e^- + O_2(g, v) \rightarrow 2e^- + O_2^+$		28	a, c
$e^- + O_2(E_x) \rightarrow 2e^- + O_2^+$		31	e
$e^- + 0 \rightarrow 2e^- + 0^+$		27	
$e^- + 0_2(g, v) \rightarrow 2e^- + 0 + 0^+$		32	a, c
$e^- + 0_2(E_x) \rightarrow 2e^- + 0 + 0^+$		32	e
$e^- + 0_3 \rightarrow 2e^- + 0 + 0_2^+$		33	
$e^{-} + 0_{3} \rightarrow e^{-} + 0^{+} + 0^{-} + 0$		27	
$e^- + 0_2(g, v) \to e^- + 0 + 0$		27	а
$e^- + 0_3 \rightarrow e^- + 0_2 + 0$		33	
$e^- + 0_2(g, v) \to 0 + 0^-$		27	a, c
$e^- + O_2(g, v) + M \rightarrow O_2^- + M$		34	a, c, f
$e^- + 0_3 \rightarrow 0^- + 0_2$		28	
$e^- + 0_3 \rightarrow 0 + 0_2^-$		28	
$e^- + O_3 + M \rightarrow O_3^- + M$	5×10^{-31}	35	f
$e^- + 0 + M \rightarrow 0^- + M$	1×10^{-31}	36	f
$e^- + NO \rightarrow 2e^- + NO^+$		37	
$e^- + NO_2 \rightarrow 2e^- + NO_2^+$		38	
$e^- + N_2 O \rightarrow 2e^- + N_2 O^+$		39	
$e^- + N_2 0 \rightarrow e^- + N_2 + 0$		40	
$e^- + N_2 0 \rightarrow e^- + N_2 + O(1D)$		40	
$e^- + N_2 O \rightarrow e^- + NO + N$		40	
$e^- + NO \rightarrow O^- + N$		37	
$e^- + N_2 0 \rightarrow N_2 + 0^-$		39	
$e^- + NO_2 \rightarrow NO_2^-$	1×10^{-11}	41	
$e^- + NO_2 \rightarrow O^- + NO$	1×10^{-11}	42	
$e^- + NO + M \rightarrow NO^- + M$	8×10^{-31}	42	f
$e^- + N_2O + M \rightarrow N_2O^- + M$	6×10^{-33}	42	f

^a For any species indicated with (g, v), g and v stand for its ground and vibrationally excited state, respectively.

^b N₂(E_x) represents the electronically excited states: N₂(A³ Σ_u^+), N₂(B³ Π_g), N₂(C³ Π_u) and N₂ (a^{'1} Σ_u^-).

^c The cross sections of the reactions involving excited species on the left hand side are shifted over the difference in the threshold energies.

 d N(E_x) represents the electronically excited states of atomic N: N(2D) and N(2P).

^e $O_2(E_x)$ represents the electronically excited states: $O_2(a^1\Delta)$, $O_2(b^1\Sigma^+)$ and a combination of three states, i.e. $O_2(A^3\Sigma^+, C^3\Delta, c^1\Sigma^-)$ at a threshold energy of 4.5 eV.

^fM represents any neutral species.

Table S.9 Neutral-neutral reactions included in the model and the corresponding rate coefficient expressions. Tg is the gas temperature in K. The rate coefficients are expressed in cm³ s⁻¹ or cm⁶ s⁻¹ for binary or ternary reactions, respectively. For certain reactions, the rate coefficients of the vibrationally excited species are determined according to the Fridman-Macheret model in which the activation energy is lowered by αE_{ν} , where α is the vibrational efficiency to lower the activation barrier and E_{ν} is the vibrational energy. For those reactions, the α parameter is given in the last column.

Reaction	Rate coefficient	Ref.	Note
$N_2(g,v) + M \rightarrow N + N + M$	$8.37 \times 10^{-4} \times \left(\frac{T_g}{T_g}\right)^{-3.5} \times$	43	a, b
	(298)		$\alpha = 1$
	$\exp\left(-\frac{T_g}{T_g}\right)$		
$N + N + M \rightarrow N_2 + M$	$1.38 \times 10^{-33} \times \exp\left(\frac{502.978}{T_{g}}\right)$	44	b
$N + N \rightarrow N_2^+ + e^-$	$2.7 \times 10^{-11} \times \exp\left(-\frac{6.74 \times 10^4}{T_g}\right)$	42	
$N + N + N \rightarrow N_2(A^3\Sigma_u^+) + N$	1.0×10^{-32}	42	
$N + N + N \rightarrow N_2 (B^3 \Pi_g) + N$	1.4×10^{-32}	42	
$N + N + N_2 \rightarrow N_2(A^3\Sigma_u^+) + N_2$	1.7×10^{-33}	42	
$N + N + N_2 \rightarrow N_2 (B^3 \Pi_g) + N_2$	2.4×10^{-33}	42	
$N(2D) + M \rightarrow N + M$	2.4×10^{-14}	45	b
$N(2P) + N \rightarrow N(2D) + N$	1.8×10^{-12}	42	
$N(2P) + N_2 \rightarrow N + N_2$	2.0×10^{-18}	42	
$N_2 \left(a^{'1} \Sigma_u^-\right) + N \rightarrow N_2 + N$	2.0×10^{-11}	46	
$\overline{N_2\left(a^{'1}\Sigma_u^-\right) + N_2 \rightarrow N_2 + N_2}$	3.7×10^{-16}	46	
$\overline{N_2(a'^1\Sigma_u^-) + N_2 \rightarrow N_2(B^3\Pi_g) + N_2}$	1.9×10^{-13}	42	
$N_2(a^{'1}\Sigma_u^-) + N_2(a^{'1}\Sigma_u^-) \rightarrow N_2^+ +$	5.0×10^{-13}	46	
$N_2 + e^-$			
$N_2(a'^1\Sigma_u^-) + N_2(a'^1\Sigma_u^-) \rightarrow N_4^+ +$	1.0×10^{-11}	42	
e ⁻			
$\overline{N_2\left(a^{'1}\Sigma_u^-\right) + N_2(A^3\Sigma_u^+) \rightarrow N_4^+ + e^-}$	$4.0 imes 10^{-12}$	42	
$N_2(A^3\Sigma_u^+) + N \rightarrow N_2 + N(2P)$	$4.0 \times 10^{-11} \times \left(\frac{300}{T_g}\right)^{0.667}$	42	
$N_2(A^3\Sigma_u^+) + N \rightarrow N_2 + N$	2.0×10^{-12}	42	
$\overline{N_2(A^3\Sigma_u^+) + N_2 \rightarrow N_2 + N_2}$	3.0×10^{-16}	42	
			-

$N_2(A^3\Sigma_u^+) + N_2(a^{'1}\Sigma_u^-) \rightarrow N_2^+ +$	1.0×10^{-12}	46	
$N_2 + e^-$			
$N_2(A^3\Sigma_u^+) + N_2(A^3\Sigma_u^+) \rightarrow N_2 +$	2.0×10^{-12}	46	
$N_2(A^3\Sigma_u^+)$			
$N_2(A^3\Sigma_u^+) + N_2(A^3\Sigma_u^+) \rightarrow N_2 +$	3.0×10^{-10}	42	
$N_2(B^3\Pi_g)$			
$N_2(A^3\Sigma_u^+) + N_2(A^3\Sigma_u^+) \rightarrow N_2 +$	1.5×10^{-10}	42	
$N_2(C^3\Pi_u)$			
$N_2(B^3\Pi_g) + N_2 \rightarrow N_2 + N_2$	2.0×10^{-12}	42	
$N_2(B^3\Pi_g) + N_2 \rightarrow N_2(A^3\Sigma_u^+) + N_2$	3×10^{-11}	42	
$N_2(C^3\Pi_u) + N_2 \rightarrow N_2 + (a'^1\Sigma_u)$	1.0×10^{-11}	42	
$O_2(g,v) + M \rightarrow 0 + 0 + M$	$\left(\frac{3.0 \times 10^{-6}}{10^{-6}}\right) \times \exp\left(\frac{-59380}{10^{-6}}\right)$		а
	(T _g) T _g)		$\alpha = 1$
$0 + 0 + M \rightarrow 0_2 + M$	$5.21 \times 10^{-35} \times \exp\left(\frac{900}{T_{g}}\right)$	47	b
$0 + 0_3 \rightarrow 0_2 + 0_2$	$8.0 \times 10^{-12} \times \exp\left(-\frac{2056}{T_g}\right)$	48	
$0 + O_2(g, v) + M \rightarrow O_3 + M$	$1.34 \times 10^{-34} \times \left(\frac{T_g}{298}\right)^{-1.0}$	49	a, b
$0_3 + M \rightarrow 0_2 + 0 + M$	$7.16 \times 10^{-10} \times \exp\left(-\frac{98120}{R_{g}T_{g}}\right)$	50	b, c
$0 + O_2(E_x) + M \rightarrow O_3 + M$	$1.34 \times 10^{-34} \times \left(\frac{T_g}{298}\right)^{-1.0}$	49	b, d, e
$0 + 0_3 \rightarrow 0_2 + 0_2(a^1\Delta)$	$2.0 \times 10^{-11} \times \exp\left(-\frac{2280}{T_g}\right)$	42	
$0_2(a^1\Delta) + 0 \rightarrow 0_2 + 0$	7.0×10^{-16}	42	
$0_2(a^1\Delta) + 0_2 \rightarrow 0_2 + 0_2$	$3.8 \times 10^{-18} \times \exp\left(-\frac{205}{T_{g}}\right)$	42	
$0_2(b^1\Sigma^+) + 0 \rightarrow 0_2(a^1\Delta) + 0$	8.1×10 ⁻¹⁴	42	
$0_2(b^1\Sigma^+) + 0 \to 0_2 + 0(1D)$	$3.4 \times 10^{-11} \times \left(\frac{T_g}{200}\right)^{-0.1} \times$	42	
	$\exp\left(-\frac{4200}{T_g}\right)$		
$0_2(b^1\Sigma^+) + 0_2 \rightarrow 0_2 + 0_2(a^1\Delta)$	$4.3 \times 10^{-22} \times (T_g)^{2.4} \times$	42	
	$\exp\left(-\frac{281}{T_g}\right)$		
$0_2(b^1\Sigma^+) + 0_3 \rightarrow 0_2 + 0_2 + 0_2$	2.2×10^{-11}	42	
$0_2(a^1\Delta) + 0_3 \rightarrow 0_2 + 0_2 + 0(1D)$	$5.2 \times 10^{-11} \times \exp\left(-\frac{2840}{T_g}\right)$	42	
$0_2(a^1\Delta) + 0_2(a^1\Delta) \rightarrow 0_2 + 0_2(a^1\Delta) \rightarrow 0_2($	$7.0 \times 10^{-28} \times \left(T_{g}\right)^{3.8} \times \exp\left(\frac{700}{T_{g}}\right)$	42	
$U_2(U \perp)$	(-g)		

$0(1D) + 0 \rightarrow 0 + 0$	8.0×10^{-12}	42	
$0(1D) + 0_2 \rightarrow 0 + 0_2$	$6.4 \times 10^{-12} \times \exp\left(-\frac{67}{T_{g}}\right)$	42	
$0(1S) + 0 \rightarrow 0(1D) + 0(1D)$	$5.0 \times 10^{-11} \times \exp\left(-\frac{300}{T_g}\right)$	42	
$0(1S) + 0_2 \rightarrow 0 + 0_2$	$1.3 \times 10^{-12} \times \exp\left(-\frac{850}{T_g}\right)$	42	
$0(1S) + 0_2 \rightarrow 0 + 0 + 0$	3.0×10^{-12}	42	
$0(1S) + 0_2(a^1\Delta) \to 0 + 0 + 0$	3.2×10^{-11}	42	
$0(1S) + O_2(a^1\Delta) \rightarrow O(1D) +$	2.9×10^{-11}	42	
$O_2(b^1\Sigma^+)$			
$0(1S) + 0_2 \rightarrow 0 +$	$3.0 \times 10^{-12} \times \exp\left(-\frac{850}{2}\right)$	42	f
$O_2(A^3\Sigma^+, C^3\Delta, c^1\Sigma^-)$	T_g		
$N + O_2(g, v) \rightarrow 0 + NO$	$2.36 \times 10^{-11} \times \exp\left(-\frac{44230}{10}\right)$	51	a, c
	$\operatorname{Lie o } (\operatorname{Rg} T_g)$		$\alpha =$
			0.24
$0 + N_2(g, v) \rightarrow N + NO$	$3.01 \times 10^{-10} \times \exp\left(-\frac{318000}{1000}\right)$	52	a, c
	r (R _g T _g)		$\alpha = 1$
$0_3 + N \rightarrow NO + 0_2$	$5.0 imes 10^{-12} imes \exp\left(-rac{650}{T_{g}} ight)$	48	
$0_3 + NO \rightarrow 0_2 + NO_2$	$2.5 \times 10^{-13} \times \exp\left(-\frac{765}{T_g}\right)$	42	
$0_3 + NO_2 \rightarrow O_2 + NO_3$	$1.2 \times 10^{-13} \times \exp\left(-\frac{2450}{T_{g}}\right)$	41	
$\mathrm{NO}_3 + \mathrm{O}_3 \rightarrow \mathrm{NO}_2 + \mathrm{O}_2 + \mathrm{O}_2$	1.0×10^{-17}	53	
$N + NO \rightarrow O + N_2$	1.66×10^{-11}	54	
$N + NO_2 \rightarrow 0 + 0 + N_2$	9.1×10^{-13}	42	
$N + NO_2 \rightarrow 0 + N_2O$	3.0×10^{-12}	42	
$N + NO_2 \rightarrow N_2 + O_2$	7.0×10^{-13}	42	
$N + NO_2 \rightarrow NO + NO$	2.3×10^{-12}	42	
$0 + NO \rightarrow N + O_2$	$7.5 \times 10^{-12} \times \left(\frac{T_g}{300}\right) \times$	42	
	$\exp\left(-\frac{19500}{T_g}\right)$		
$0 + NO_2 \rightarrow NO + O_2$	$9.05 \times 10^{-12} \times \left(\frac{T_g}{298}\right)^{-0.52}$	55	
$0 + N_2 0 \rightarrow N0 + N0$	$1.5 imes 10^{-10} imes \exp\left(-rac{14090}{T_g} ight)$	42	
$0 + N_2 0 \rightarrow N_2 + O_2$	$8.3 \times 10^{-12} \times \exp\left(-\frac{14000}{T_{g}}\right)$	42	
$0 + NO_3 \rightarrow O_2 + N_2$	1.0×10^{-11}	42	

$NO + NO \rightarrow N + NO_2$	$3.3 \times 10^{-16} \times \left(\frac{300}{T_{g}}\right)^{0.5} \times$	42	
	$\exp\left(-\frac{39200}{T_g}\right)$		
$NO + NO \rightarrow O + N_2O$	$2.2 \times 10^{-12} \times \exp\left(-\frac{32100}{T_g}\right)$	42	
$NO + NO \rightarrow N_2 + O_2$	$5.1 \times 10^{-13} \times \exp\left(-\frac{33660}{T_{g}}\right)$	42	
$NO + N_2O \rightarrow N_2 + NO_2$	$4.6 imes 10^{-10} imes \exp\left(-rac{25170}{T_g} ight)$	42	
$NO + NO_3 \rightarrow NO_2 + NO_2$	1.7×10^{-11}	42	
$NO_2 + NO_2 \rightarrow NO + NO_3$	$4.5 \times 10^{-10} \times \exp\left(-\frac{18500}{T_{g}}\right)$	42	
$NO_2 + NO_2 \rightarrow NO + NO + O_2$	$3.3 \times 10^{-12} \times \exp\left(-\frac{13500}{T_g}\right)$	42	
$NO_2 + NO_3 \rightarrow NO + NO_2 + O_2$	$2.3 \times 10^{-13} \times \exp\left(-\frac{1600}{T_{g}}\right)$	42	
$\mathrm{NO}_3 + \mathrm{NO}_3 \rightarrow \mathrm{O}_2 + \mathrm{NO}_2 + \mathrm{NO}_2$	$4.3 \times 10^{-12} \times \exp\left(-\frac{3850}{T_g}\right)$	42	
$NO + O_2(g, v) \rightarrow O + NO_2$	$2.8 \times 10^{-12} \times \exp\left(-\frac{23400}{T_{g}}\right)$	⁴² a α	= 1
$NO + NO + O_2(g, v) \rightarrow NO_2 + NO_2$	$3.3 \times 10^{-39} \times \exp\left(-\frac{4410}{R_{g}T_{g}}\right)$	⁵⁶ a, α	c = 0.2

$NO_2 + O_2(g, v) \rightarrow NO + O_3$	$2.8 \times 10^{-12} \times \exp\left(-\frac{25400}{2}\right)$	42	а
	' (T _g)		$\alpha = 0.2$
$\mathrm{NO}_3 + \mathrm{O}_2(\mathrm{g},\mathrm{v}) \rightarrow \mathrm{O}_3 + \mathrm{NO}_2$	$1.5 \times 10^{-12} \times \exp\left(-\frac{15020}{2}\right)$	42	а
	' (T _g /		$\alpha = 0.8$
$NO + O \rightarrow NO_2$	$3.01 \times 10^{-11} \times \left(\frac{T_g}{300}\right)^{-0.75}$	57	
$NO_2 + NO + M \rightarrow N_2O_3 + M$	$3.09 \times 10^{-34} \times \left(\frac{T_{g}}{300}\right)^{-7.70}$	48	b
$NO_2 + NO_2 + M \rightarrow N_2O_4 + M$	$1.4 \times 10^{-33} \times \left(\frac{T_{g}}{300}\right)^{-3.8}$	48	b
$\mathrm{NO}_2 + \mathrm{NO}_3 + \mathrm{M} \rightarrow \mathrm{N}_2\mathrm{O}_5 + \mathrm{M}$	$3.7 \times 10^{-30} \times \left(\frac{300}{T_g}\right)^{4.10}$	56	b
$N + O + M \rightarrow NO + M$	$1.0 \times 10^{-32} \times \left(\frac{300}{T_g}\right)^{0.5}$	42	b
$N_2(g,v) + 0 + M \rightarrow N_2 0 + M$	$3.9 \times 10^{-35} \times \exp\left(-\frac{10400}{T_g}\right)$	42	b
$N_2 0 + M \rightarrow N_2 + 0 + M$	$1.20 \times 10^{-9} \times \exp\left(-\frac{240000}{R_{g}T_{g}}\right)$	42	b, c

$NO_2 + M \rightarrow NO + O + M$	$9.4 \times 10^{-5} \times \left(\frac{T_g}{298}\right)^{-2.66} \times$	57	b, c
	$\exp\left(-\frac{311000}{R_{g}T_{g}}\right)$		
$NO_3 + M \rightarrow NO + O_2 + M$	$2.51 \times 10^{-14} \times \exp\left(-\frac{10230}{R_{g}T_{g}}\right)$	58	b, c
$NO + M \rightarrow N + O + M$	$8.7 imes 10^{-9} imes \exp\left(-rac{75994}{T_g} ight)$	42	b
$N_2O_3 + M \rightarrow NO + NO_2 + M$	$1.91 \times 10^{-7} \times \left(\frac{T_g}{298}\right)^{-8.7} \times$	48	b, c
	$\exp\left(-\frac{40570}{R_gT_g}\right)$		
$N_2O_4 + M \rightarrow NO_2 + NO_3 + M$	$1.3 \times 10^{-5} \times \left(\frac{T_g}{298}\right)^{-3.8} \times$	48	b, c
	$\exp\left(-\frac{53210}{R_{g}T_{g}}\right)$		
$N_2O_5 + M \rightarrow NO_2 + NO_3 + M$	$2.1 \times 10^{-11} \times \left(\frac{300}{T_g}\right)^{-3.5} \times$	42	b, c
	$\exp\left(-\frac{91460}{R_{g}T_{g}}\right)$		
$NO + O_2(g, v) + M \rightarrow NO_3 + M$	$5.65 \times 10^{-41} \times \exp\left(-\frac{1750}{R_{g}T_{g}}\right)$	59	a, b, c
$NO + O_2(E_x) + M \rightarrow NO_3 + M$	$5.65 \times 10^{-41} \times \exp\left(-\frac{1750}{R_g T_g}\right)$	59	b, d
$N + N + NO \rightarrow N_2(A^3\Sigma_u^+) + NO$	1.7×10^{-33}	42	
$N + N + NO \rightarrow N_2(B^3\Pi_g) + NO$	2.4×10^{-33}	42	
$N + N + 0 \rightarrow N_2(A^3\Sigma_u^+) + 0$	1.0×10^{-32}	42	
$N + N + 0 \rightarrow N_2 (B^3 \Pi_g) + 0$	1.4×10^{-32}	42	
$N + N + O_2 \rightarrow N_2(A^3\Sigma_1^+) + O_2$	1.7×10^{-33}	42	
$N + N + O_2 \rightarrow N_2(B^3\Pi_g) + O_2$	2.4×10^{-33}	42	
$N(2D) + N_2O \rightarrow NO + N_2$	3.5×10^{-12}	42	
$N(2D) + NO \rightarrow N_2 + O$	1.8×10^{-10}	42	
$N(2D) + 0 \rightarrow N + O(1D)$	4.0×10^{-13}	42	
$N(2D) + O_2(g, v) \rightarrow NO + O$	5.2×10^{-12}	42	а
$N(2P) + NO \rightarrow N_2(A^3\Sigma_u^+) + O$	3.0×10^{-11}	42	
$N(2P) + 0 \rightarrow N + 0$	1.0×10^{-12}	42	
$N(2P) + O_2(g, v) \rightarrow NO + O$	2.6×10^{-15}	42	а
$N_2(a'^1\Sigma_u^-) + NO \rightarrow N_2 + N + O$	3.6×10^{-10}	42	
$N_2(a'^1\Sigma_u^-) + 0 \rightarrow NO + N$	3.0×10^{-10}	52	
$N_2(a'^1\Sigma_u^-) + O_2(g,v) \to N_2 + 0 + 0$	2.8×10^{-11}	42	a
$N_2(A^3\Sigma_u^+) + N_2O \rightarrow N_2 + N + NO$	1.0×10^{-11}	42	

$N_2(A^3\Sigma_u^+) + NO \rightarrow N_2 + NO$	6.9×10^{-11}	42	
$N_2(A^3\Sigma_u^+) + NO_2 \rightarrow N_2 + 0 + NO$	1.0×10^{-12}	42	
$N_2(A^3\Sigma_u^+) + 0 \rightarrow N_2 + 0(1S)$	2.1×10^{-11}	42	
$N_2(A^3\Sigma_u^+) + 0 \rightarrow NO + N(2D)$	7.0×10^{-12}	42	
$N_2(A^3\Sigma_u^+) + O_2(g,v) \to N_2 + 0 + 0$	$2.0 \times 10^{-12} \times \left(\frac{T_g}{300}\right)^{0.55}$	42	a
$N_2(A^3\Sigma_u^+) + O_2 \rightarrow N_2 + O_2(a^1\Delta)$	$2.0 \times 10^{-13} \times \left(\frac{T_g}{300}\right)^{0.55}$	42	
$N_2(A^3\Sigma_u^+) + O_2 \rightarrow N_2 + O_2$	2.54×10^{-12}	42	
$N_2(A^3\Sigma_u^+) + O_2(g,v) \to N_2O + O$	$2.0 \times 10^{-14} \times \left(\frac{T_g}{300}\right)^{0.55}$	42	а
$N_2(B^3\Pi_g) + N_2O \rightarrow N_2 + N + NO$	0.58×10^{-10}	60	
$N_2(B^3\Pi_g) + N_2O \rightarrow N_2 + N_2 + O$	0.58×10^{-10}	60	
$N_2(B^3\Pi_g) + 0 \rightarrow NO + N$	3.0×10^{-10}	52	
$N_2(C^3\Pi_u) + 0 \rightarrow NO + N$	3.0×10^{-10}	52	
$N_2(C^3\Pi_u) + O_2(g,v) \rightarrow N_2 + 0 + 0$	3.0×10^{-10}	42	а
$\mathrm{NO} + \mathrm{O}_2(\mathrm{E}_\mathrm{x}) \to \mathrm{O} + \mathrm{NO}_2$	$2.8 \times 10^{-12} \times \exp\left(-\frac{23400}{T_{g}}\right)$	42	d, g
$\mathrm{NO}_3 + \mathrm{O}_2(\mathrm{E}_\mathrm{x}) \rightarrow \mathrm{O}_3 + \mathrm{NO}_2$	$1.5 \times 10^{-12} \times \exp\left(-\frac{15020}{T_g}\right)$	42	d, h
$0(1D) + N_2 \rightarrow N_2 + 0$	2.3×10^{-11}	42	
$0(1S) + N \rightarrow 0 + N$	1.0×10^{-12}	42	
$0(1S) + N_2(g, v) \rightarrow 0 + N_2(g, v)$	1.0×10^{-17}	42	
$O_2(a^1\Delta) + N \rightarrow NO + O$	$2.0 \times 10^{-14} \times \exp\left(-\frac{600}{T_{g}}\right)$	42	
$0_2(a^1\Delta) + N_2(g,v) \rightarrow 0_2 + N_2(g,v)$	3.0×10^{-21}	42	
$O_2(a^1\Delta) + NO \rightarrow O_2 + NO$	2.5×10^{-11}	42	
$O_2(b^1\Sigma^+) + N_2 \rightarrow O_2(a^1\Delta) + N_2$	$1.7 \times 10^{-15} \times \left(\frac{T_g}{300}\right)^{1.0}$	42	
$N_2(B^3\Pi_g) + NO \rightarrow N_2(A^3\Sigma_u^+) + NO$	2.4×10^{-10}	42	
$N_2(B^3\Pi_g) + O_2(g, v) \rightarrow N_2 + 0 + 0$	3.0×10^{-10}	42	a

^a For any species indicated with (g, v), g and v stand for its ground and vibrationally excited state, respectively.

^b M represents any neutral species.

^c $R_g = 8.3144598 \text{ J. K}^{-1} \text{ mol}^{-1}$ is the universal gas constant.

 d O₂(E_x) represents the two electronically excited states: O₂(a¹ Δ) and O₂(b¹ Σ ⁺).

^e The rate coefficient is assumed to be equal to the rate of $0 + 0_2 + M \rightarrow 0_3 + M$.

^fO₂(A³ Σ^+ , C³ Δ , c¹ Σ^-) is a combination of three electronic excited states at a threshold energy of 4.5 eV.

^g The rate coefficient is assumed to be equal to the rate of $NO + O_2 \rightarrow O + NO_2$.

^h The rate coefficient is assumed to be equal to the rate of $NO_3 + O_2 \rightarrow O_3 + NO_2$.

Table S.10 Electron-ion recombination reactions included in the model and the corresponding rate coefficient expressions. Te is to the electron temperature in K and Tg is the gas temperature in K. The rate coefficients are expressed in $\text{cm}^3 \text{ s}^{-1}$ or $\text{cm}^6 \text{ s}^{-1}$ for binary or ternary reactions, respectively.

Reaction	Rate coefficient	Ref.	Note
$e^- + N_2^+ \rightarrow N + N(g, E_x)$	$R \times 1.8 \times 10^{-7} \times \left(\frac{300}{T_e}\right)^{0.39}$	42	а
$e^- + N_3^+ \rightarrow N_2 + N$	$2 \times 10^{-7} \times \left(\frac{300}{T_e}\right)^{0.5}$	61	
$e^- + N_3^+ \rightarrow N_2(E_x) + N$	$6.91 \times 10^{-8} \times \left(\frac{T_e}{11604.5}\right)^{-0.5}$	61	С
$e^- + N_4^+ \rightarrow N_2 + N_2$	$2.3 \times 10^{-6} \times \left(\frac{300}{T_e}\right)^{0.53}$	42	
$e^- + N_4^+ \rightarrow N_2 + N + N$	$3.13 \times 10^{-7} \times \left(\frac{T_e}{11604.5}\right)^{-0.41}$	61	
$e^- + N^+ + e^- \rightarrow e^- + N$	$7 \times 10^{-20} \times \left(\frac{300}{T_{e}}\right)^{4.5}$	61	
$e^- + N^+ + M \rightarrow N + M$	$6 \times 10^{-27} \times \left(\frac{300}{T_{e}}\right)^{1.5}$	62	b
$e^- + N_2^+ + e^- \rightarrow e^- + N_2$	$1 \times 10^{-19} \times \left(\frac{T_e}{300}\right)^{-4.5}$	61	
$e^- + N_2^+ + M \rightarrow N_2 + M$	$2.49 \times 10^{-29} \times \left(\frac{T_e}{11604.5}\right)^{-1.5}$	61	b
$e^- + 0^+ + 0_2 \rightarrow 0 + 0_2$	$6 \times 10^{-27} \times \left(\frac{300}{T_{e}}\right)^{1.5}$	62	
$e^- + 0^+ + e^- \rightarrow e^- + 0$	$7 \cdot 10^{-20} \cdot \left(\frac{300}{T_e}\right)^{4.5}$	42	
$e^{-} + O_{2}^{+} + M \rightarrow O_{2} + M$	1×10^{-26}	36	b
$e^- + 0_2^+ + e^- \rightarrow e^- + 0_2$	$1 \times 10^{-19} \times \left(\frac{T_e}{300}\right)^{-4.5}$	62	
$e^- + 0^+_2 \to 0 + 0$	$6.46 \times 10^{-5} \times T_e^{-0.5} \times T_g^{-0.5}$	63	
$e^- + 0^+_2 \rightarrow 0 + 0(1D)$	$1.08 \times 10^{-7} \left(\frac{T_e}{300}\right)^{-0.7}$	42	
$e^- + 0^+_2 \rightarrow 0 + 0(1S)$	$0.14 \times 10^{-7} \left(\frac{T_e}{300}\right)^{-0.7}$	42	
$e^- + 0^+_4 \rightarrow 0^2 + 0^2$	$1.4 \times 10^{-6} \times \left(\frac{300}{T_e}\right)^{0.5}$	42	
$e^- + NO^+ + e^- \rightarrow e^- + NO$	$1.0 \times 10^{-19} \left(\frac{T_e}{300}\right)^{-4.5}$	62	
$e^- + NO^+ + M \rightarrow NO + M$	$2.49 \times 10^{-29} \times \left(\frac{T_e}{11604.5}\right)^{-1.5}$	61	b

$e^- + NO^+ \rightarrow O + N(g, E_x)$	$R \times 4.2 \times 10^{-7} \times \left(\frac{300}{T_e}\right)^{0.85}$	⁴² d
$e^- + N_2 0^+ \rightarrow N_2 + 0$	$2.0 \times 10^{-7} \times \left(\frac{300}{T_{e}}\right)^{0.5}$	42
$e^- + NO_2^+ \rightarrow NO + O$	$2.0 \times 10^{-7} \times \left(\frac{300}{T_{e}}\right)^{0.5}$	42
$e^{-} + O_2^+ N_2 \rightarrow O_2 + N_2$	$1.3 \times 10^{-6} \times \left(\frac{300}{T_{e}}\right)^{0.5}$	42

^a In N(g, E_x), g stands for the ground state of atomic N and E_x represents two of its electronically excited states: N(2D) and N(2P); R is equal to 0.5, 0.45 and 0.05 for N, N(2D) and N(2P), respectively.

^b M represents any neutral species.

^c N₂(E_x) represents N₂(A³ Σ_{u}^{+}) and N₂(B³ Π_{g}).

^d In N(g, E_x), g stands for the ground state of atomic N and E_x represents the electronic excited state N(2D); R is equal to 0.2 and 0.8 for N and N(2D), respectively.

Table S.11 Ion-neutral reactions included in the model and the corresponding rate coefficient expressions. T_g is the gas temperature in K. For certain reactions, T_{ion} is the effective temperature of the reacting ion in K [26]. The rate coefficients are expressed in cm³ s⁻¹ or cm⁶ s⁻¹ for binary or ternary reactions, respectively.

Reaction	Rate coefficient	Ref.	Note
$N_2^+ + N \rightarrow N^+ + N_2$	$7.2 \times 10^{-13} \times \left(\frac{\mathrm{T_{ion}}}{\mathrm{300}}\right)$	42	
$N_2^+ + N + N_2 \rightarrow N_3^+ + N_2$	$9.0 \times 10^{-30} \times \left(\frac{400}{\mathrm{T_{ion}}}\right)$	42	
$N_4^+ + N_2 \rightarrow N_2^+ + N_2 + N_2$	$2.1 \times 10^{-16} \times \left(\frac{\text{Tion}}{121}\right)$	42	
$N^+ + N_2 + N_2 \rightarrow N_3^+ + N_2$	$1.7 \times 10^{-29} \times \left(\frac{300}{\text{Tion}}\right)^{2.1}$	42	
$N_2^+ + N_2 + N_2 \rightarrow N_4^+ + N_2$	$5.2 \times 10^{-29} \times \left(\frac{300}{T_{\rm ion}}\right)^{2.2}$	42	
$N^+ + N + N_2 \rightarrow N_2^+ + N_2$	1.0×10^{-29}	42	
$N^+ + N \rightarrow N_2^+$	1.0×10^{-29}	64	
$N_3^+ + N \rightarrow N_2^+ + N_2$	6.6×10^{-11}	42	
$\overline{\mathrm{N}_4^+ + \mathrm{N} \rightarrow \mathrm{N}^+ + \mathrm{N}_2 + \mathrm{N}_2}$	1.0×10^{-11}	42	
$N_2^+ + N_2(A^3\Sigma_u^+) \to N_3^+ + N$	3.0×10^{-10}	41	
$0^- + M \rightarrow 0 + M + e^-$	4.0×10^{-12}	41	а
$0^- + 0 \to 0_2 + e^-$	2.3×10^{-10}	65	
$0^- + 0_2(g, v) + M \rightarrow 0_3^- + M$	$1.1 \times 10^{-30} \times \exp\left(\frac{300}{T_g}\right)$	65	a, b

$0^- + 0_2(g, v) \rightarrow 0_3 + e^-$	5.0×10^{-15}	42	b
$0^- + 0_3 \rightarrow 0_2 + 0_2 + e^-$	3.0×10^{-10}	66	
$0^- + 0_3 \rightarrow 0_3^- + 0$	5.3×10^{-10}	67	
$0^+ + 0 + M \rightarrow 0^+_2 + M$	1.0×10^{-29}	62	а
$0^+ + 0_2(g, v) \to 0 + 0_2^+$	$1.9 \times 10^{-11} \times \left(\frac{T_g}{300}\right)^{-0.5}$	68	b
$0^+ + 0_3 \rightarrow 0_2^+ + 0_2$	1.0×10^{-10}	62	
$O_2^- + M \rightarrow O_2 + M + e^-$	$2.7 \times 10^{-10} \times \left(\frac{T_g}{300}\right)^{0.5} \times$	68	a
	$\exp\left(-\frac{5590}{T_g}\right)$		
$0_2^- + 0 \to 0_2 + 0^-$	3.31×10^{-10}	65	
$0_2^- + 0_2(g, v) + M \rightarrow 0_4^- + M$	$3.5 \times 10^{-31} \times \left(\frac{T_g}{300}\right)^{-1.0}$	62,65,67	a, b
$0_2^- + 0_2 \rightarrow 0_2 + 0_2 + e^-$	2.18×10^{-18}	69	
$0_2^- + 0_3 \rightarrow 0_3^- + 0_2$	4.0×10^{-10}	65	
$O_2^+ + O_2(g, v) + M \rightarrow O_4^+ + M$	$2.4 \times 10^{-30} \times \left(\frac{T_g}{300}\right)^{-3.2}$	62	a, b
$0_3^- + M \rightarrow 0_3 + M + e^-$	2.3×10^{-11}	68	а
$0_3^- + 0 \rightarrow 0_2^- + 0_2^- + e^-$	1.0×10^{-13}	67	
$0_3^- + 0 \to 0_2^- + 0_2$	2.5×10^{-10}	35	
$0_3^- + 0 \to 0_3^- + 0^-$	1.0×10^{-13}	65	
$0_3^- + 0_3 \rightarrow 0_2 + 0_2 + 0_2 + e^-$	3.0×10^{-10}	67	
$0_4^- + 0 \rightarrow 0^- + 0_2 + 0_2$	3.0×10^{-10}	62	
$0_{4}^{-} + 0 \rightarrow 0_{3}^{-} + 0_{2}$	4.0×10^{-10}	62	
$0_4^- + 0_2 \rightarrow 0_2^- + 0_2 + 0_2$	$1.0 \times 10^{-10} \times \exp\left(-\frac{1044}{T_g}\right)$	42	
$0_4^+ + 0 \rightarrow 0_2^+ + 0_3$	3.0×10^{-10}	62	
$0_4^+ + 0_2 \rightarrow 0_2^+ + 0_2 + 0_2$	$3.3 \times 10^{-6} \times \left(\frac{300}{T_{g}}\right)^{4.0} \times$	62	
	$\exp\left(-\frac{5030}{T_g}\right)$		
$0^- + 0_2(a^1\Delta) \to 0_3 + e^-$	3.0×10^{-10}	42	
$0_2^- + 0_2(a^1\Delta) \to 0_2 + 0_2 + e^-$	2.0×10^{-10}	42	
$0_2^- + 0_2(b^1\Sigma^+) \rightarrow 0_2^- + 0_2^- + e^-$	3.6×10^{-10}	42	
$O_2^+ + O_2(E_x) + M \to O_4^+ + M$	$2.4 \times 10^{-30} \times \left(\frac{T_g}{300}\right)^{-3.2}$	42	a, c, d
$0_4^+ + 0_2(a^1\Delta) \rightarrow 0_2^+ + 0_2 + 0_2$	1.0×10^{-10}	42	
$0_4^- + 0_2(E_x) \rightarrow 0_2^- + 0_2 + 0_2$	1.0×10^{-10}	42	с
$0^- + 0_2(a^1\Delta) \to 0_2^- + 0$	1.0×10^{-10}	42	

$0^- + 0_2(E_x) + M \rightarrow 0_3^- + M$	$1.1 \times 10^{-30} \times \exp\left(rac{300}{T_g} ight)$	42	a, c, e
$0_2^- + 0_2(E_x) + M \to 0_4^- + M$	$3.5 \times 10^{-31} \times \exp\left(\frac{T_g}{300}\right)^{-1.0}$	62	a, c, f
$N^+ + N + O_2 \rightarrow N_2^+ + O_2$	1.0×10^{-29}	42	
$N^+ + N_2 O \rightarrow NO^+ + N_2$	5.5×10^{-10}	42	
$N^+ + NO \rightarrow N_2^+ + O$	3.0×10^{-12}	42	
$N^+ + NO \rightarrow NO^+ + N$	8.0×10^{-10}	42	
$N^+ + NO \rightarrow O^+ + N_2$	1.0×10^{-12}	42	
$N^+ + O + M \rightarrow NO^+ + M$	1.0×10^{-29}	42	а
$N^+ + O \rightarrow N + O^+$	1.0×10^{-12}	42	
$N^+ + O_2 \rightarrow NO^+ + O$	2.5×10^{-10}	42	
$N^+ + O_2 \rightarrow O^+ + NO$	2.8×10^{-11}	42	
$N^+ + O_2 \rightarrow O_2^+ + N$	2.8×10^{-10}	42	
$N^+ + O_3 \rightarrow NO^+ + O_2$	5.0×10^{-10}	42	
$N_2^+ + N_2 O \rightarrow N_2 O^+ + N_2$	5.0×10^{-10}	42	
$N_2^+ + N_2 O \rightarrow NO^+ + N + N_2$	4.0×10^{-10}	42	
$N_2^+ + NO \rightarrow NO^+ + N_2$	3.3×10^{-10}	42	
$N_2^+ + 0 \rightarrow N0^+ + N$	$1.3 \times 10^{-10} \times \left(\frac{300}{T_{\rm ion}}\right)^{0.5}$	42	
$N_2^+ + O_2 \rightarrow O_2^+ + N_2$	$6.0 \times 10^{-11} \times \left(\frac{300}{T_{\rm ion}}\right)^{0.5}$	42	
$N_2^+ + O_3 \rightarrow O_2^+ + O + N_2$	1.0×10^{-10}	42	
$N_2O^- + N \rightarrow NO + N_2 + e^-$	5.0×10^{-10}	41	
$N_2O^- + O \rightarrow NO + NO + e^-$	1.5×10^{-10}	41	
$N_20^+ + N0 \rightarrow N0^+ + N_20$	2.9×10^{-10}	42	
$N_3^+ + NO \rightarrow N_2O^+ + N_2$	7.0×10^{-11}	42	
$N_3^+ + NO \rightarrow NO^+ + N + N_2$	7.0×10^{-11}	42	
$N_3^+ + O_2 \rightarrow NO_2^+ + N_2$	4.4×10^{-11}	42	
$N_3^+ + O_2 \rightarrow O_2^+ + N + N_2$	2.3×10^{-11}	42	
$N_4^+ + NO \rightarrow NO^+ + N_2 + N_2$	4.0×10^{-10}	42	
$N_4^+ + 0 \rightarrow 0^+ + N_2 + N_2$	2.5×10^{-10}	42	
$N_4^+ + O_2 \rightarrow O_2^+ + N_2 + N_2$	2.5×10^{-10}	42	
$N0^- + N_20 \rightarrow N0 + N_20 + e^-$	$4.26 \times 10^{-10} \times \exp\left(-\frac{107.2}{T_g}\right)$	70	
$NO^- + NO \rightarrow NO + NO + e^-$	$3.28 \times 10^{-10} \times \exp\left(-\frac{105.1}{T_g}\right)$	70	
$N0^- + N \rightarrow N_20 + e^-$	5.0×10^{-10}	42	
$NO^- + N_2O \rightarrow NO_2^- + N_2$	2.8×10^{-14}	42	

$NO^- + NO_2 \rightarrow NO_2^- + NO$	7.4×10^{-10}	42	
$NO^- + O \rightarrow NO_2 + e^-$	1.5×10^{-10}	41	
$NO^- + O_2 \rightarrow O_2^- + NO$	5.0×10^{-10}	42	
$NO_2^- + N \rightarrow NO + NO + e^-$	5.0×10^{-10}	41	
$\overline{\mathrm{NO}_2^- + \mathrm{N}_2\mathrm{O}_5} \rightarrow \mathrm{NO}_3^- + \mathrm{NO}_2 + \mathrm{NO}_2$	7.0×10^{-10}	42	
$NO_2^- + NO_2 \rightarrow NO_3^- + NO$	4.0×10^{-12}	42	
$NO_2^- + NO_3 \rightarrow NO_3^- + NO_2$	5.0×10^{-10}	42	
$NO_2^- + O_3 \rightarrow NO_3^- + O_2$	1.8×10^{-11}	42	
$NO_2^+ + NO \rightarrow NO^+ + NO_2$	2.9×10^{-10}	42	
$NO_3^- + N \rightarrow NO + NO_2 + e^-$	5.0×10^{-10}	41	
$NO_3^- + NO \rightarrow NO_2^- + NO_2$	3.0×10^{-15}	42	
$NO_3^- + 0 \rightarrow NO + O_3 + e^-$	1.5×10^{-10}	41	
$0^- + N \rightarrow NO + e^-$	2.6×10^{-10}	42	
$0^- + N_2(g, v) \rightarrow N_2 0 + e^-$	0.5×10^{-13}	42	b
$0^- + N_2(A^3\Sigma_u^+) \to 0 + N_2 + e^-$	2.2×10^{-9}	42	
$0^- + N_2 (B^3 \Pi_g) \rightarrow 0 + N_2 + e^-$	1.9×10^{-9}	42	
$0^- + N_2 0 \rightarrow N_2 0^- + 0$	2.0×10^{-12}	42	
$0^- + N_2 0 \rightarrow N0^- + N0$	2.0×10^{-10}	42	
$0^- + NO + M \rightarrow NO_2^- + M$	1.0×10^{-29}	42	а
$0^- + NO \rightarrow NO_2 + e^-$	2.6×10^{-10}	42	
$0^- + NO_2 \rightarrow NO_2^- + 0$	1.2×10^{-9}	42	
$0^+ + N + M \rightarrow N0^+ + M$	1.0×10^{-29}	42	а
$0^+ + N \rightarrow N^+ + 0$	1.3×10^{-10}	42	
$0^{+} + N_2(g, v) + M$	$(300)^2$	42	a, b
$\rightarrow NO^{+} + N + M$	$6.0 \times 10^{-29} \times \left(\frac{1}{T_{ion}}\right)$		
$0^+ + N_2(g, v) \rightarrow N0^+ + N$	$(1.5 - 2.0 \times 10^{-3} \times T_{ion} +$	42	b
	$9.6 \times 10^{-7} \times T_{ion}^2) \times 1.0 \times 10^{-7}$		
	10 ⁻¹²		
$0^+ + N_2 0 \rightarrow N_2 0^+ + 0$	2.2×10^{-10}	42	
$0^+ + N_2 0 \rightarrow N0^+ + N0$	2.3×10^{-10}	42	
$0^+ + N_2 0 \rightarrow 0_2^+ + N_2$	2.0×10^{-11}	42	
$0^+ + N0 \rightarrow N0^+ + 0$	2.4×10^{-11}	42	
$0^+ + NO \rightarrow 0^+_2 + N$	3.0×10^{-12}	42	
$0^+ + \mathrm{NO}_2 \rightarrow \mathrm{NO}_2^+ + 0$	1.6×10^{-9}	42	
$0_2^- + N \rightarrow NO_2 + e^-$	5.0×10^{-10}	42	
$O_2^- + N_2(B^3\Pi_g) \to O_2 + N_2 + e^-$	2.5×10^{-9}	42	
$0_2^- + N_2(A^3\Sigma_1^+) \rightarrow 0_2 + N_2 + e^-$	2.1×10^{-9}	42	
$0_3^- + N_2(B^3\Pi_g) \rightarrow 0_3 + N_2 + e^-$	2.5×10^{-9}	41	
5 4 57 5 4			

$0_3^- + N_2(A^3\Sigma_u^+) \to 0_3 + N_2 + e^-$	2.1×10^{-9}	41	
$NO^- + N_2(B^3\Pi_g)$	2.5×10^{-9}	41	
\rightarrow NO + N ₂ + e ⁻			
$NO^- + N_2(A^3\Sigma_u^+) \rightarrow NO + N_2 + e^-$	2.1×10^{-9}	41	
$N_2 0^- + N_2 (B^3 \Pi_g)$	2.5×10^{-9}	41	
\rightarrow N ₂ 0 + N ₂ + e ⁻			
$N_2 0^- + N_2 (A^3 \Sigma_{\mu}^+)$	2.1×10^{-9}	41	
$\rightarrow N_2 0 + N_2 + e^-$			
$NO_2^- + N_2 (B^3 \Pi_g)$	2.5×10^{-9}	41	
$\rightarrow NO_2 + N_2 + e^-$			
$NO_2^- + N_2(A^3\Sigma_u^+)$	2.1×10^{-9}	41	
$\rightarrow NO_2 + N_2 + e^-$			
$NO_3^- + N_2 (B^3 \Pi_g)$	2.5×10^{-9}	41	
\rightarrow NO ₃ + N ₂ + e ⁻			
$NO_3^- + N_2(A^3\Sigma_u^+)$	2.1×10^{-9}	41	
$\rightarrow NO_3 + N_2 + e^-$			
$0_2^- + \mathrm{NO}_2 \to \mathrm{NO}_2^- + \mathrm{O}_2$	$7.0 imes 10^{-10}$	42	
$0_2^- + \mathrm{NO}_3 \rightarrow \mathrm{NO}_3^- + \mathrm{O}_2$	$5.0 imes 10^{-10}$	42	
$0_2^+ + N \rightarrow N0^+ + 0$	1.2×10^{-10}	42	
$0_2^+ + N_2(g, v) + N_2 \rightarrow 0_2^+ N_2 + N_2$	$9.0 \times 10^{-31} \times \left(\frac{300}{T_{\rm ion}}\right)^2$	42	b
$0_2^+ + N_2(g, v) \rightarrow NO^+ + NO$	1.0×10^{-17}	42	b
$0_2^+ + \text{NO} \rightarrow \text{NO}^+ + 0_2$	6.3×10^{-10}	42	
$0_2^+ + \mathrm{NO}_2 \rightarrow \mathrm{NO}^+ + \mathrm{O}_3$	1.0×10^{-11}	42	
$0_2^+ + \mathrm{NO}_2 \rightarrow \mathrm{NO}_2^+ + \mathrm{O}_2$	$6.6 imes 10^{-10}$	42	
$O_2^+N_2^- + N_2^- \rightarrow O_2^+ + N_2^- + N_2^-$	$1.1 \times 10^{-6} \times \left(\frac{300}{T_{ion}}\right)^{5.3}$	42	
	$\times \exp\left(-\frac{2360}{T_{ion}}\right)$		
$O_2^+ N_2^- + O_2^- \rightarrow O_4^+ + N_2^-$	1.0×10^{-9}	42	
$\overline{O_3^- + N} \rightarrow NO + O_2 + e^-$	5.0×10^{-10}	41	
$0_3^- + \mathrm{NO} \rightarrow \mathrm{NO}_2^- + \mathrm{O}_2$	2.6×10^{-12}	42	
$\overline{\text{O}_3^- + \text{NO} \rightarrow \text{NO}_3^- + \text{O}}$	1.0×10^{-11}	42	
$0_3^- + \mathrm{NO}_2 \to \mathrm{NO}_2^- + \mathrm{O}_3$	$7.0 imes 10^{-11}$	42	
$0_3^- + \mathrm{NO}_2 \to \mathrm{NO}_3^- + \mathrm{O}_2$	2.0×10^{-11}	42	
$0_{\overline{2}}^{-} + NO_{2} \rightarrow \overline{NO_{\overline{2}}^{-}} + O_{2}$			
03 1 1103 1 103 1 03	5.0×10^{-10}	42	

$0_4^- + \text{NO} \rightarrow \text{NO}_3^- + \text{O}_2$	2.5×10^{-10}	42
$0_4^+ + N_2(g, v) \rightarrow 0_2^+ N_2 + 0_2$	$4.6 \times 10^{-12} \times \left(\frac{T_{\text{ion}}}{300}\right)^{2.5}$	⁴² b
	$\times \exp\left(-\frac{2650}{T_{ion}}\right)$	
$0_4^+ + \mathrm{NO} \rightarrow \mathrm{NO^+} + \mathrm{O_2} + \mathrm{O_2}$	1.0×10^{-10}	42

^a M represents any neutral species.

^b For any species indicated with (g, v), g and v stand for its ground and vibrationally excited state, respectively.

^c $O_2(E_x)$ represents the electronically excited states: $O_2(a^1\Delta)$ and $O_2(b^1\Sigma^+)$.

^d The rate coefficient is assumed to be equal to the rate of $O_2^+ + O_2^- + M \rightarrow O_4^+ + M$.

^e The rate coefficient is assumed to be equal to the rate of $0^- + 0_2 + M \rightarrow 0_3^- + M$.

^f The rate coefficient is assumed to be equal to the rate of $0_2^- + 0_2 + M \rightarrow 0_4^- + M$.

Table S.12 Ion-ion reactions included in the model, the corresponding rate coefficient expressions and the references. T_g is the gas temperature in K. The rate coefficients are expressed in $cm^3 s^{-1} or cm^6 s^{-1}$ for binary or ternary reactions, respectively.

Reaction	Rate coefficient	Ref.	Note
$0^{-} + 0^{+} + M \rightarrow 0_{2} + M$	$1.0 imes 10^{-25} imes \left(rac{300}{T_g} ight)^{2.5}$	68	a
$0^- + 0_2^+ + M \to 0_3 + M$	$1.0 \times 10^{-25} \times \left(\frac{300}{T_g}\right)^{2.5}$	68	а
$0_2^- + 0^+ + M \to 0_3 + M$	$1.0 imes 10^{-25} imes \left(rac{300}{T_{g}} ight)^{2.5}$	68	a
$0_2^- + 0_2^+ + M \rightarrow 0_2 + 0_2 + M$	$1.0 imes 10^{-25} imes \left(rac{300}{T_{g}} ight)^{2.5}$	68	a
$0_3^- + 0^+ + M \rightarrow 0_3 + 0 + M$	$2.0 \times 10^{-25} \times \left(\frac{300}{T_{g}}\right)^{2.5}$	41	a
$0_3^- + 0_2^+ + M \to 0_3 + 0_2 + M$	$2.0 \times 10^{-25} \times \left(\frac{300}{T_{g}}\right)^{2.5}$	41	a
$0^- + 0^+_2 \to 0 + 0 + 0$	$2.60 \times 10^{-8} \times \left(\frac{300}{T_g}\right)^{0.44}$	65	a
$0_3^- + 0_2^+ \to 0 + 0 + 0_3$	$1.0 \times 10^{-7} \times \left(\frac{300}{T_g}\right)^{0.5}$	65	a

$0^- + 0^+ \to 0 + 0$	$4.0 \times 10^{-8} \times \left(\frac{300}{T_g}\right)^{0.43}$	65	
$0^- + 0^+_2 \to 0^2 + 0$	$2.6 \times 10^{-8} \times \left(\frac{300}{T_g}\right)^{0.44}$	65	
$0_2^- + 0^+ \to 0 + 0_2$	$2.7 \times 10^{-7} \times \left(\frac{300}{T_{g}}\right)^{0.5}$	65	
$0_2^- + 0_2^+ \to 0_2^- + 0_2^-$	$2.01 \times 10^{-7} \times \left(\frac{300}{T_g}\right)^{0.5}$	65	
$0_2^- + 0_2^+ \to 0_2^- + 0 + 0$	$1.01 \times 10^{-13} \times \left(\frac{300}{T_g}\right)^{0.5}$	65	
$0_3^- + 0^+ \to 0_3 + 0$	$1.0 \times 10^{-7} \times \left(\frac{300}{T_{g}}\right)^{0.5}$	69	
$0_3^- + 0_2^+ \to 0_2 + 0_3$	$2.0 \times 10^{-7} \times \left(\frac{300}{T_g}\right)^{0.5}$	65	
$NO^- + A^+ + M \rightarrow NO + A + M$	$2.0 \times 10^{-25} \times \left(\frac{300}{T_g}\right)^{2.5}$	41	a, b
$NO_2^- + A^+ + M \rightarrow NO_2 + A + M$	$2.0 \times 10^{-25} \times \left(\frac{300}{T_g}\right)^{2.5}$	41	a, b
$N_2O^- + A^+ + M \rightarrow N_2O + A + M$	$2.0 \times 10^{-25} \times \left(\frac{300}{T_g}\right)^{2.5}$	41	a, b
$NO_3^- + A^+ + M \rightarrow NO_3 + A + M$	$2.0 \times 10^{-25} \times \left(\frac{300}{T_g}\right)^{2.5}$	41	a, b
$0_3^- + B^+ + M \to 0_3 + B + M$	$2.0 \times 10^{-25} \times \left(\frac{300}{T_g}\right)^{2.5}$	41	a, c

^a M represents any neutral species.

^b A represents N, O, N₂, O₂, NO, NO₂ and N₂O species.

^c B represents N, N₂, NO, NO₂ and N₂O species.

Table S.13 Optical transitions of N_2 and O_2 species. The rate coefficients are expressed in s^{-1} .

Reaction	Rate coefficient	Ref.	Note
$N_2(A^3\Sigma_u^+) \rightarrow N_2$	0.5	42	
$N_2(B^3\Pi_g) \rightarrow N_2(A^3\Sigma_u^+)$	1.35×10^{5}	42	
$N_2(a'^1\Sigma_u^-) \rightarrow N_2$	1.0×10^{2}	42	
$N_2(C^3\Pi_u) \to N_2(B^3\Pi_g)$	2.45×10^{7}	42	
$0_2(a^1\Delta) \rightarrow 0_2$	2.6×10^{-4}	42	
$0_2(b^1\Sigma^+) \rightarrow 0_2$	8.5×10^{-2}	42	
$0_2(b^1\Sigma^+) \rightarrow 0_2(a^1\Delta)$	1.5×10^{-3}	42	

$O_2(A^3\Sigma^+, C^3\Delta, c^1\Sigma^-) \to O_2 $ 11	42	а	
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^a $O_2(A^3\Sigma^+, C^3\Delta, c^1\Sigma^-)$ is a combination of three electronic excited states at a threshold energy of 4.5 eV.

The reaction rate expressions of the VT relaxations and VV exchanges between $N_2 - N_2$, $N_2 - O_2$ and $O_2 - O_2$ are calculated using the Forced Harmonic Oscillator (FHO) model proposed by Adamovich et al.⁷¹ This method offers a semi-classical non-perturbative analytical solution for VT and VV transitions of diatomic molecules by averaging the VT and VV probabilities (P_{VT} and P_{VV}) over the one-dimensional Boltzmann distribution.

$$P_{VT}(i \to f) = \frac{(n_s)^s}{(s!)^2} \cdot \varepsilon^s \cdot \exp\left(-\frac{2n_s}{s+1}\varepsilon\right)$$
(10)

$$P_{VV}(i_1, i_2 \to f_1, f_2) \cong \frac{\left[n_s^{(1)} n_s^{(2)}\right]^s}{(s!)^2} \cdot \left(\frac{\rho_{\epsilon}^2}{4}\right)^s \cdot \exp\left[-\frac{2n_s^{(1)} n_s^{(2)}}{s+1}\frac{\rho_{\epsilon}^2}{4}\right]$$
(11)

with s = |i - f|, $n_s = \left[\frac{\max(i, f)!}{\min(i, f)!}\right]^{1/s}$. ρ_{ε} and ε are collision and potential specific parameters.

Table S. 14 Vibrational – vibrational exchanges and vibrational – translational relaxations for N_2 (as an example) and the rate coefficient expression..

Reaction	Rate coefficient
$N_2(v_i) + M \rightarrow N_2(v_i - 1) + M$	$Z \cdot \left(\frac{m}{kT}\right) \int_0^\infty P_{VT}(\overline{v}) \cdot exp\left(\frac{-mv^2}{2kT}\right) v dv$
$N_2(v_i) + N_2(v_j) \rightarrow N_2(v_i - 1) + N_2(v_j + 1)$	$Z \cdot \left(\frac{m}{kT}\right) \int_0^\infty P_{VV}(\bar{v}) \cdot exp\left(\frac{-mv^2}{2kT}\right) v dv$
M represents any neutral particle in the plasma.	

 v_i and v_j are the vibrational levels of N_2 (0-24).

Z is the collision frequency and v is the particle velocity.

The reaction rates of the VT relaxations between $N_2 - N$ are based on quasi classical calculations that have been reproduced through a fit as proposed by Esposito et al.⁷², for the following general reaction:

 $N_2(v) + N \rightarrow N_2(w) + N$, with v > w

All the relevant trends in the rate were taken into consideration by using an additive model into the exponential argument of the reaction rate constant, as shown in the following expression (valid for v = 1 - 66 and $\Delta v = 1 - 30$):

$$K(\mathbf{v}, \mathbf{T}, \Delta \mathbf{v}) = \exp\left(a_1(\mathbf{v}, \Delta \mathbf{v}) + \frac{a_2(\mathbf{v}, \Delta \mathbf{v})}{\mathbf{T}} + \frac{a_3(\mathbf{v}, \Delta \mathbf{v})}{\mathbf{T}^2} + \frac{a_4(\mathbf{v}, \Delta \mathbf{v})}{\mathbf{T}^3} + a_5(\mathbf{v}, \Delta \mathbf{v}) \cdot \ln(\mathbf{T})\right)$$
(12)

where

$$a_{i}(v,\Delta v) = z_{i0}(\Delta v) + z_{i1}(\Delta v)v + z_{i2}(\Delta v)v^{2} + z_{i3}(\Delta v)v^{3} + z_{i4}(\Delta v)v^{4}$$
(13)

$$z_{ij}(\Delta v) = b_{ij} + c_{ij}\Delta v \tag{14}$$

For which the parameters are reported in 72 .

Similarly, the reaction rates of the VT relaxations between $O_2 - O$ are based on quasi classical calculations that have been reproduced through a fit as proposed by Esposito et al.⁷³, for the following general reaction:

 $0_2(v) + 0 \rightarrow 0_2(w) + 0$, with v > w

The reaction rate constant is then determined based on the following expression:

$$K(T, v, \Delta v) = \text{DegF} \cdot \exp(a_1(v, \Delta v) + \frac{a_2(v, \Delta v)}{\ln(T)} + a_3(v, \Delta v) \cdot \ln(T)$$
(15)

where Δv is (v - w)

$$a_{i}(v, \Delta v) = b_{i1}(\Delta v) + b_{i2}(\Delta v) \cdot \ln(v) + \frac{b_{i3}(\Delta v) + b_{i4}(\Delta v)v + b_{i5}(\Delta v)v^{2}}{10^{21} + \exp(v)}$$
(15)
$$b_{ij}(\Delta v) = c_{ij1} + c_{ij2} \cdot \ln(\Delta v) + c_{ij3} \cdot \Delta v \cdot \exp(-\Delta v) + c_{ij4} \cdot \Delta v \cdot \Delta v$$
(16)

The coefficients c_{ijk} have been generated using a linear least squares method and are reported in⁷³ where the degenary factor (DegF) is also explained.

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