

Improving Molecule–Metal Surface Reaction Networks Using the Meta-Generalized Gradient Approximation: CO₂ Hydrogenation

Yuxiang Cai,¹ Roel Michiels,¹ Federica De Luca, Erik Neyts, Xin Tu, Annemie Bogaerts, and Nick Gerrits*



Cite This: *J. Phys. Chem. C* 2024, 128, 8611–8620



Read Online

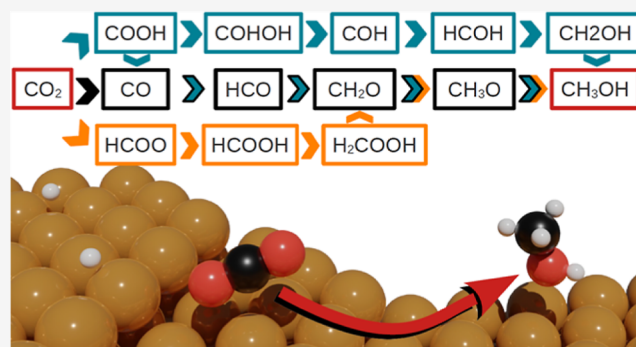
ACCESS |

Metrics & More

Article Recommendations

Supporting Information

ABSTRACT: Density functional theory is widely used to gain insights into molecule–metal surface reaction networks, which is important for a better understanding of catalysis. However, it is well-known that generalized gradient approximation (GGA) density functionals (DFs), most often used for the study of reaction networks, struggle to correctly describe both gas-phase molecules and metal surfaces. Also, GGA DFs typically underestimate reaction barriers due to an underestimation of the self-interaction energy. Screened hybrid GGA DFs have been shown to reduce this problem but are currently intractable for wide usage. In this work, we use a more affordable meta-GGA (mGGA) DF in combination with a nonlocal correlation DF for the first time to study and gain new insights into a catalytically important surface reaction network, namely, CO₂ hydrogenation on Cu. We show that the mGGA DF used, namely, rMS-RPBE-rVV10, outperforms typical GGA DFs by providing similar or better predictions for metals and molecules, as well as molecule–metal surface adsorption and activation energies. Hence, it is a better choice for constructing molecule–metal surface reaction networks.



1. INTRODUCTION

Climate change is one of the most important challenges humanity faces in the 21st century. To limit global warming, it is essential to reduce carbon dioxide (CO₂) emissions.¹ The catalytic hydrogenation of CO₂ to methanol (CH₃OH) is of particular interest as CH₃OH is considered both a clean fuel and a versatile feedstock for green chemistry.² Despite the industrialization of this technology, the underlying mechanism remains poorly understood.² A common challenge pertains to the identification of the reaction sites and the carbon species' evolution in the reaction network. The latter bears critical implications for the development of novel CO₂ hydrogenation processes, such as electrocatalysis and plasma catalysis.

Density functional theory (DFT) has been widely used to gain insights into the energetics and mechanisms of catalytic reactions on surfaces. Moreover, the results of such DFT studies can also be used in kinetic and multiscale modeling of catalytic reactions. However, it is difficult to determine the exact surface mechanism of most catalytic reactions using DFT. This is, in part, due to the dependency of the results on the choice of density functional (DF).³ Most studies use generalized gradient approximation (GGA) DFs, i.e., DFs that only depend on the electron density and its gradient. However, GGA DFs are known to struggle to simultaneously provide accurate predictions of both molecular gas-phase and metal surface energies,⁴ where both are crucial for the study of

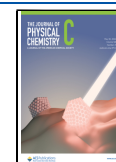
reactions at metal surfaces. Specifically, GGA DFs that excel at describing adsorption energies tend to underestimate the energy of the metal surface itself and overestimate the metal lattice constant, while GGA DFs that perform well for metals tend to overestimate adsorption energies.⁵ Furthermore, GGA DFs tend to systematically underestimate barrier heights.⁶ To address these limitations, meta-GGA (mGGA) DFs introduce a dependency on the kinetic energy density (KED). This allows them to distinguish between regions with electron densities describing molecular orbitals, metallic orbitals, and weak bonds, resulting in a DF that can accurately describe both metal surfaces and gas-phase molecules. Several mGGA DFs^{7–10} also have a hydrogen self-interaction error (SIE) correction, i.e., a parameter is introduced that is fitted so the DF reproduces the exact exchange energy of a free hydrogen atom. This yields an approximate correction in the molecular orbital regime to the SIE inherent to DFT. This interaction of an electron with itself arises due to the use of the classical expression for the Coulomb interaction of electron densities.

Received: February 20, 2024

Revised: May 7, 2024

Accepted: May 9, 2024

Published: May 17, 2024



The introduction of the KED also allows us to satisfy additional theoretical constraints compared to GGA DFs.^{4,10,11} Besides the choice of DF, when studying surface reaction networks, it can also be important to explicitly compute reaction barriers as the use of scaling relations can be problematic. For example, it has been found that the SIE tends to be lower for adsorption than for the transition state (TS),⁶ meaning that the DF behaves differently for the calculation of adsorption energies and activation energy barriers, necessitating the explicit calculation of the barrier.¹² Lastly, it is vital to comprehensively study the reaction network as a whole and not one possible mechanism separately as this leads to the a priori exclusion of other mechanisms. In this work, we will study a surface reaction network for the first time using a mGGA DF and illustrate that the mGGA DF outperforms GGA DFs in the description of the system, namely, CO₂ hydrogenation toward CH₃OH over a Cu surface.

Several DFT studies on the reaction mechanism of CO₂ hydrogenation toward CH₃OH on Cu were previously carried out.^{13–20} The active site for this reaction is still unclear, so we will discuss both the flat Cu(111) and stepped Cu(211) surfaces as the possible pathways investigated in literature are the same for both facets. All possible pathways are depicted in a reaction network in Figure 1. In the formate pathway, in pink,

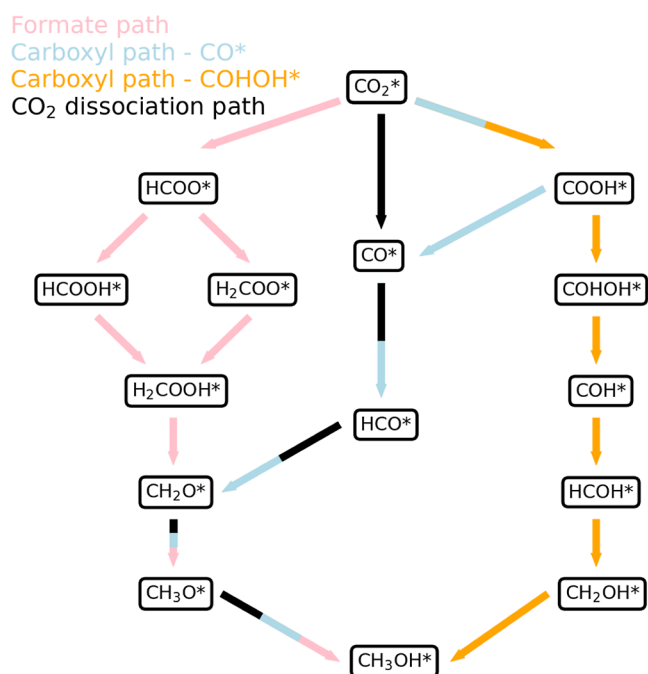


Figure 1. Overview of possible pathways from CO₂ to CH₃OH on Cu(111) and Cu(211) surfaces. The formate path is indicated in pink, the carboxyl path through CO* in blue, the carboxyl path through COHOH* in orange, and the CO₂ dissociation path in black.

CO₂* (* denotes adsorbed species) is hydrogenated to HCOO* and subsequently either to HCOOH* or H₂COO*. In the carboxyl pathway, CO₂* is hydrogenated to COOH*, which can either dissociate to CO* and OH*, in blue, or be hydrogenated to COHOH*, in orange. Finally, in the CO₂ dissociation pathway, in black, CO₂* dissociates into CO* and O* without going through another intermediate first. It is worth noting that most of the aforementioned studies did not comprehensively investigate all reaction pathways mentioned above simultaneously but rather focused on one or a few

possible reaction mechanisms. Furthermore, all of them employed a GGA DF.

Studt et al.²¹ compared two GGA DFs, i.e., BEEF-vdW²² and revised Perdew–Burke–Ernzerhof (RPBE),²³ for the description of CO₂ hydrogenation on Cu(211). They concluded that BEEF-vdW improves the description of CH₃OH synthesis and partially attributed this to the inclusion of long-range correlation effects in the BEEF-vdW DF, which are missing in the semilocal RPBE DF. However, it is important to note that they apply an empirical correction to the energies of species containing an OCO backbone. It is unclear to us to what degree these corrections are responsible for the improved performance of BEEF-vdW. Nevertheless, the inclusion of long-range nonlocal correlation and the importance of van der Waals forces have also been suggested by Garza et al.²⁴ to improve the description of chemisorption on metal surfaces, also when using a mGGA DF.

It is clear that for a good description of reaction networks on metal surfaces, a mGGA DF combined with the inclusion of long-range correlation is needed. One way to construct a mGGA DF is by introducing an inhomogeneity parameter α associated with the KED, which allows the DF to distinguish between the different density regimes associated with the metal surface and the gas-phase molecule. Unfortunately, the choice of mGGA DF is also not trivial. For example, the strongly constrained and appropriately normed (SCAN)⁸ DF has been shown to greatly underestimate molecule–metal surface reaction barrier heights.^{10,25} A recent development in this field is the made-simple (MS) DFs.^{7,10,26} In these DFs, an interpolation function dependent on α is used to switch between the metallic and atomic regimes, where a correction to the atomic regime is made to reproduce the exact exchange energy of a free hydrogen atom.

The first MS DF, MS0,²⁶ was found to outperform the standard PBE²⁷ GGA DF in predicting exchange energies of rare gas atoms, atomization energies, enthalpies of formation, and lattice constants. It was found to perform similarly to the revTPSS²⁸ mGGA. MS0²⁶ was later parameterized by including one or two empirical parameters, resulting in the MS1 and MS2 DFs, respectively.⁷ Overall, MS1 and MS2 were found to improve over MS0, and all MS DFs showed robust performance in predicting heats of formation, barrier heights, and weak interactions.⁷ The performance of these MS DFs was compared to that of GGA DFs, including PBE,²⁷ and to that of mGGA DFs, including M06-L²⁹ and revTPSS.²⁸ MS1 was found to perform best in predicting a set of heats of formation, while M06-L was found to perform best in predicting a set of barriers, closely followed by MS0, MS1, and MS2.²⁹ The authors noted that the number of parameters in M06-L is an order of magnitude larger than the number of parameters in the MS DFs.²⁹ These results show that the MS DFs are robust and perform well in describing gas-phase molecules.

Smeets et al.¹⁰ recently proposed three MS mGGA DFs (MS-PBEI, MS-B86bI, and MS-RPBEI) based on the exchange expressions of PBE,²⁷ B86b,³⁰ and RPBE²³ but with the exchange gradient expansion coefficient μ taken from PBEsol.³¹ The GGA correlation expression was taken from revTPSS.²⁸ They studied the decomposition of H₂ on Cu(111) and Ag(111) surfaces and found that these DFs exhibit similar accuracy to PBEsol in predicting the properties of metallic Cu and Ag while outperforming both the GGA DFs PBE and RPBE and mGGA DFs SCAN⁸ and TPSS⁹ in predicting experimental molecular beam sticking probabilities on

Cu(111). Furthermore, they found that DFs excellently predicted the experimental interlayer lattice spacing for Cu and Ag and the lattice parameter for Pt and Au. Recently, the performance of MS-B86bl was investigated in the SBH17 benchmarking study, a database for dissociative chemisorption barrier heights.²⁵ It was found that the DF performed well for predicting metal properties. Moreover, for 16 of the 17 studied dissociative chemisorption systems, MS-B86bl yielded accurate saddle point geometries and a mean absolute error of 0.17 eV for the dissociation barrier heights, only failing to obtain a self-consistent saddle point for H₂ + Pt(211), which is a very shallow barrier and difficult to obtain with both GGA and mGGA DFs. Although MS-B86bl was found to be a somewhat mediocre DF compared to other (m)GGA DFs for SBH17, it should also be noted that SBH17 only contains reactions for which GGA DFs excel^{6,25} and that MS-B86bl lacks long-range correlation. For example, MS-RPBE has also been used to describe dissociative chemisorption of O₂ on Al(111)⁶ and HCl on Au(111),³² two infamous examples where all GGA DFs severely overestimate the reactivity. In general, they yielded considerably improved agreement with experimental sticking and inelastic scattering probabilities compared to GGA DFs. Moreover, in a later study, Smeets and Kroes³³ combined these MS mGGA DFs with rVV10,³⁴ a self-consistent nonlocal correlation DF. As mentioned above, the inclusion of nonlocal correlation is critical for a good description of reaction networks on metal surfaces. The inclusion of rVV10 slightly reduced the accuracy of the metal description but improved the description of D₂ dissociative adsorption on Ag(111), Pt(111), and Au(111). MS-PBE-rVV10 was later used to study CHD₃ dissociation on a Pt(110)-(2 × 1) surface and led to good agreement with experimental results.³⁵ The above shows that the combination of a high-accuracy mGGA DF with rVV10 overcomes the limitations of GGA DFs by solving the challenges of the description in metal surface layers and of the molecule and including long-range interactions, critical when describing adsorption.^{21,24} Moreover, the computational cost of a mGGA DF is roughly a factor three more than that of a GGA DF, making it a cost-effective option for constructing comprehensive and self-consistent reaction networks.

Here, we use a regularization of the inhomogeneity parameter α , which is used in most mGGA DFs, that was introduced in r²SCAN.³⁶ This regularization improved the numerical performance of the SCAN functional while maintaining its accuracy, which is observed here as well, i.e., the regularization does not affect the results. Note that the regularized parameter is only used in the exchange part of the DF as revTPSS GGA correlation is employed in the MS mGGA DFs, which does not contain the α parameter.

To the best of our knowledge, no mGGA DF has so far been applied for the study of a reaction network on any metal surface. Hence, in this work, we will use an MS mGGA DF, i.e., regularized MS-RPBE, combined with rVV10 nonlocal correlation (rMS-RPBE-rVV10), to study CO₂ hydrogenation on Cu(111) and Cu(211). We hope, and indeed conclude, that this will lead to a better understanding due to the improved description of both the metal and molecule by the MS mGGA DFs and the inclusion of nonlocal correlation via rVV10. To evaluate the performance of the rMS-RPBE-rVV10 DF on this reaction network, three GGA-level DFs with vdW correction, namely, PBE-D3,^{27,37} RPBE-D3,^{23,37} and BEEF-vdW²² were chosen for comparison.

2. METHODS

Periodic plane-wave DFT calculations were carried out using the Vienna ab initio simulation package (VASP, version 6.2.1).^{38–43} The regularized MS RPBE-like (rMS-RPBE)¹⁰ mGGA DF was used in combination with the rVV10³⁴ DF to account for nonlocal correlation effects. This gives the following expression for the exchange–correlation functional³³

$$E_{XC}^{\text{rMS-RPBE-rVV10}} = E_X^{\text{rMS-RPBE}} + E_C^{\text{revTPSS}} + E_C^{\text{non-local}}$$

where $E_X^{\text{rMS-RPBE}}$ is the MS-RPBE exchange DF, E_C^{revTPSS} is the semilocal revTPSS²⁸ GGA correlation DF (i.e., GGA instead of mGGA correlation is employed), and $E_C^{\text{non-local}}$ is the non-local rVV10³⁴ correlation DF. For a detailed explanation on the latter two parts of the DF, we refer the reader to the respective references. $E_X^{\text{rMS-RPBE}}$ is given by²⁶

$$E_X^{\text{rMS-RPBE}} = \int d^3r n \epsilon_x^{\text{unif}}(n) F_x^{\text{rMS-RPBE}}(p, \bar{\alpha})$$

$$\epsilon_x^{\text{unif}}(n) = \frac{-3 \left(\frac{9\pi}{4}\right)^{1/3}}{r_s}$$

$$r_s = \left(\frac{4\pi n}{3}\right)^{-1/3}$$

$$p = s^2 = \frac{|\nabla n|^2}{4(3\pi^2)^{2/3} n^{8/3}}$$

Here, n is the density and ϵ_x^{unif} is the exchange energy per particle of a uniform electron gas (UEG). The exchange enhancement factor $F_x^{\text{rMS-RPBE}}$ is given by ref 33 as

$$F_x^{\text{rMS-RPBE}}(p, \bar{\alpha}) = F_{x,\text{RPBE}}^1(p) + f(\bar{\alpha})(F_{x,\text{RPBE}}^0(p; c) - F_{x,\text{RPBE}}^1(p))$$

The exchange enhancement factor is used to obtain the exchange part of the exchange–correlation energy by interpolating between two extreme cases: the UEG and a single-orbital system. $F_{x,\text{RPBE}}^1(p)$ and $F_{x,\text{RPBE}}^0(p; c)$ are the gradient-only-dependent exchange enhancement factors for the UEG and single-orbital cases, respectively. The former is expressed as

$$F_{x,\text{RPBE}}^1(p) = 1 + \kappa(1 - e^{-\mu p/\kappa})$$

For $F_{x,\text{RPBE}}^0$, μp is replaced in the formula above by $\mu p + c$. μ is 10/81, κ is 0.804, and c is 0.07671. For a more detailed explanation of the parameter values, we refer the reader to the publication by Smeets et al.¹⁰ The interpolation function $f(\bar{\alpha})$ depends on the KED τ through the inhomogeneity parameter α ^{10,36}

$$f(\bar{\alpha}) = \frac{1 - \bar{\alpha}^2}{1 + \bar{\alpha}^3 + \bar{\alpha}^5}$$

$$\bar{\alpha} = \frac{\alpha}{1 + \eta^5 p} = \frac{\tau - \tau^W}{\tau^{\text{unif}} + \eta \tau^W}$$

where τ^W is the von Weizsäcker KED, τ^{unif} is the KED of the UEG, and η is a regularization parameter equal to 0.001. Expressions for these KEDs can be found in the paper by Sun et al.²⁶ In the single-orbital case, which is a good model for covalent bonding, $\bar{\alpha} = 0$ because $\tau^W = \tau$, and thus $f(\bar{\alpha}) = 1$.

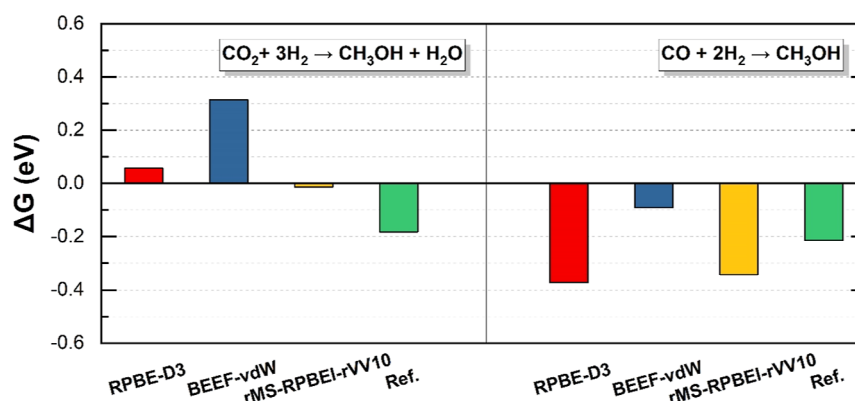


Figure 2. Comparison of ΔG in CO₂ (left) and CO (right) hydrogenation calculated by RPBE-D3, BEEF-vdW, and rMS-RPBE-rVV10 with the reference value.³ The thermal correction is at 500 K and the pressures of CO₂, CO, H₂, H₂O, and CH₃OH are 10, 10, 40, 1, and 1 bar, respectively.

This leads to the exchange energy being determined only by the single-orbital exchange enhancement factor F_x^0 . In the UEG case, which is a good model for metallic bonding, $\bar{\alpha}$ approaches 1 because $\tau \approx \tau^{\text{unif}}$ and $\tau^{\text{W}} \ll \tau^{\text{unif}}$, and thus $f(\bar{\alpha}) = 0$. This leads to the exchange energy only being determined by the UEG exchange enhancement factor F_x^1 . Hence, the interpolation function and inhomogeneity parameter allow the functional to switch between different density regimes.

The expression for $\bar{\alpha}$ is taken from r²SCAN³⁶ and is a regularized form of the expression used by Smeets et al.¹⁰ This regularization leads to a numerically more stable functional and mainly affects convergence in cases that are more difficult to converge due to a singularity in the nonregularized form of the inhomogeneity parameter. The regularization does not affect the results but only improves the numerical performance. We would like to emphasize that rMS-RPBE-rVV10 is not a new DF. We have only introduced the regularization of the inhomogeneity parameter from r²SCAN³⁶ into the MS-RPBE-rVV10 DF designed by Smeets et al.¹⁰ Additionally, a different regularization of the iso-orbital indicator in the MS2 DF has been tried by Furness and Sun, where similar observations have been made.⁴⁴

Two GGA DFs were also used to evaluate the performance of the rMS-RPBE-rVV10 DF, namely, RPBE²³ with Grimme's D3 nonlocal correction³⁷ and Bayesian error estimation functional with nonlocal van der Waals correlation^{22,45} (BEEF-vdW). These GGA DFs were only used for calculations on the Cu(111) slab. The core electrons were described by the projector-augmented wave method.^{46,47} A plane-wave kinetic energy cutoff of 600 eV was used for the plane-wave basis set, and the energy in the self-consistent field was converged to within 10⁻⁷ eV.

The Cu lattice constant is optimized using a Γ -centered 20 × 20 × 20 k -point mesh. The force on each atom is converged to within 0.005 eV/Å. The lattice constant computed with the rMS-RPBE-rVV10 DF is 3.52 Å, which is the same value as the one reported by Smeets and Kroes³³ and is in good agreement with the experimental value of 3.60 Å.⁴⁸ For the BEEF-vdW and RPBE-D3 DFs, the lattice constants are 3.66 and 3.58 Å, respectively.

The Cu(211) and Cu(111) surfaces are both modeled as a 3 × 3 periodic 6-layer slab with a 16 Å vacuum region placed between periodically repeated slabs. During the calculations, the three upper layers and adsorbates are fully relaxed, while the lower layers remain fixed at equilibrium bulk positions. For both slabs, a Γ -centered 4 × 4 × 1 k -point mesh is used for

sampling the Brillouin zone. The force on each atom is converged to within 0.01 eV/Å. First, the interlayer distance is optimized with these settings. For the Cu(111) slab, only the z -coordinate of the atoms of the top three layers is allowed to relax, while the x - and y -coordinates are fixed. In all other calculations, all coordinates are relaxed. The distance between the top two layers in the Cu(111) slab increases by 1.8% for the rMS-RPBE-rVV10 functional, which is in good agreement with the value reported by Smeets and Kroes,³³ i.e., an increase of 1.6%. For the BEEF-vdW and RPBE-D3 DFs, the interlayer distance decreased by 1.0% and increased by 1.1%, respectively. The distance between the top two 111 layers in the Cu(211) slab increased with 3.8% for the rMS-RPBE-rVV10 DF.

TSs are obtained using the dimer method as implemented in the VASP TS tools^{49–52} package and are confirmed to be first-order saddle points by checking if only one imaginary frequency is found in the normal-mode analysis. In TS searches for dissociative chemisorption reactions, the surface was fixed to the optimized geometry as in these reactions the surface does not have enough time to rearrange.

The adsorption energy of species, E_{ads} , is defined as

$$E_{\text{ads}} = E_{\text{adsorbate+surface}} - (E_{\text{surface}} + E_{\text{adsorbate}})$$

where $E_{\text{adsorbate+surface}}$, E_{surface} , and $E_{\text{adsorbate}}$ are the total energies of the adsorbate on the slab, the clean Cu slab, and the gaseous adsorbate, respectively. The convergence of the calculation parameters is tested and is provided in Supporting Information S.1.

3. RESULTS AND DISCUSSION

3.1. Comparison of DFs. The calculated Cu lattice constants of RPBE-D3, BEEF-vdW, and rMS-RPBE-rVV10 are 3.575, 3.664, and 3.525 Å, respectively, while the experimental value is 3.597 Å.⁴⁸ The inclusion of vdW corrections influences the prediction of the lattice constant, i.e., the lattice constant tends to decrease when including vdW corrections, which is beneficial for RPBE and unfavorable for the MS mGGA DFs,¹⁰ as they accurately predict the lattice constant without vdW corrections, while RPBE overestimates the lattice constant. Among the studied DFs, BEEF-vdW is found to overestimate the lattice constant, while RPBE-D3 and rMS-RPBE-rVV10 demonstrate underestimation. Both the RPBE-D3 and the BEEF-vdW lattice constants are slightly closer to the experimental value than the value predicted by

Table 1. Adsorption Energies, Dissociation Barriers, and Preferred Binding Sites of Relevant Species on Cu(111), Calculated with RPBE-D3, BEEF-vdW, and rMS-RPBEL-rVV10^a

	RPBE-D3	BEEF-vdW	rMS-RPBEL-rVV10	site	ref value (eV)
Adsorption Energy (eV)					
CO	-0.84	-0.53	-0.87	fcc	-0.57 ⁵⁴
H ₂ O	-0.39	-0.19	-0.25	top	-0.40 ⁵⁵
HCOOH	-0.53	-0.26	-0.38	top	-0.55 ⁵⁶
CH ₂ O	-0.33	-0.16	-0.25	hcp	-0.10 ⁵⁷
CH ₃ OH	-0.51	-0.26	-0.38	top	-0.60 ⁵⁸
CO ₂	-0.26	-0.17	-0.12	phys	-0.25 ⁵⁹
H ₂	-0.10	-0.05	-0.02	phys	-0.03 ⁶⁰
Dissociation Barrier (eV)					
H ₂	0.47	0.94	0.57	bridge	0.63 ²⁵
CO ₂	1.34	1.55	1.29	fcc	0.96 ⁶¹
Errors (eV)					
MSD	-0.08	0.15	0.02		
MAD	0.11	0.17	0.15		

^aPhys indicates physisorbed species. The CO₂ dissociation barrier is not taken into account for the calculation of the MAD and MSD.

rMS-RPBEL-rVV10. Nevertheless, all exhibit reasonable predictions.

In Figure 2, the change of the Gibbs free energy (ΔG) was calculated for the gas-phase reactions $\text{CO}_2 + 3\text{H}_2 \rightarrow \text{CH}_3\text{OH} + \text{H}_2\text{O}$ and $\text{CO} + 2\text{H}_2 \rightarrow \text{CH}_3\text{OH}$, represented as ΔG_{CO_2} and ΔG_{CO} , respectively, utilizing three DFs. Thermodynamic corrections (see S.2 in Supporting Information) were applied for typical operating conditions in the industrial hydrogenation of CO₂ to methanol. These conditions include a temperature of 500 K and pressures of CO₂, CO, H₂, H₂O, and CH₃OH at 10, 10, 40, 1, and 1 bar, respectively. The obtained results indicate that all three DFs give reasonable predictions of ΔG_{CO} , with BEEF-vdW overestimating ΔG_{CO} (i.e., not negative enough) with 0.12 eV, rMS-RPBEL-rVV10 underestimating ΔG_{CO} with 0.13 eV, and RPBE-D3 underestimating ΔG_{CO} with 0.16 eV. For ΔG_{CO_2} , on the other hand, both BEEF-vdW and RPBE-D3 predict the reaction to be thermodynamically unfavorable, which can likely be ascribed to inaccuracies in addressing the O–C–O backbone with GGA DFs. Hence, corrections of gas-phase molecules are typically necessary for CO₂-related studies based on GGA DFs.^{21,53} Of the used DFs, rMS-RPBEL-rVV10 offers the most accurate prediction of ΔG_{CO_2} by predicting an exothermic reaction. Furthermore, the difference between ΔG_{CO_2} and ΔG_{CO} is also best predicted by rMS-RPBEL-rVV10. In short, rMS-RPBEL-rVV10 does not only yield reasonable predictions for metal surfaces but also for gas-phase molecules, which is fundamentally not possible with GGA DFs.⁴

Now, we turn to the adsorption of important reaction intermediates on a Cu(111) surface by again comparing the aforementioned DFs. The most favorable adsorption sites, i.e., the sites with the lowest adsorption energy, along with their respective adsorption energies are presented in Table 1. All three DFs predict the same adsorption sites. Both H₂ and CO₂ demonstrate weak adsorption on the surface, exhibiting physisorption characteristics in line with previously reported findings.^{62,63} A more complete overview of adsorbed intermediates calculated with rMS-RPBEL-rVV10 on Cu(111) and Cu(211) can be found in S.3 in Supporting Information.

In terms of the adsorption energy of CO, rMS-RPBEL-rVV10 and RPBE-D3 predict a considerably lower energy compared to that of the experiment (cf. ref. value in last column). The

adsorption energies predicted by RPBE-D3, BEEF-vdW, and rMS-RPBEL-rVV10 are -0.84, -0.53, and -0.87 eV, respectively. An experimental value of -0.57 eV was reported by Hinch and Dubois using high-resolution electron-energy loss spectroscopy.⁵⁴ Notably, the description of CO adsorption on transition metal surfaces, such as Cu(111), poses significant complications in DFT calculations, a dilemma referred to as the “CO adsorption puzzle”.^{64,65} Experimental evidence has suggested a preference for CO to adsorb at the top site on Cu(111).⁶⁶ However, all three DFs employed in this study indicate that the favored adsorption site is the fcc site. This suggests that the reasonable agreement of the adsorption energy predicted by BEEF-vdW with the experiment is a consequence of cancellation of errors and not of its predictive capability. This phenomenon can be attributed to a synergistic effect of the SIE and errors driven by density approximations.⁶⁷ A notable solution to this quandary was recently provided by Mishima et al.,⁶⁸ who applied a long-range corrected hybrid DF, thereby mitigating the issue. In light of these findings, it becomes intriguing to explore the utilization of higher-level DFs, such as hybrid mGGA DFs, in order to achieve a more accurate description of reactions related to CO by minimizing the influence of the SIE. To the best of our knowledge, no hybrid GGA studies of a CO₂ reaction network on a Cu surface are available in literature. Hence, there is no comparison with such a study in this work. Also, for the foreseeable future, such DFs are intractable, due to their computational cost, for computing an entire reaction network that includes explicitly the barrier heights.

For H₂ and CO₂, energy barriers for dissociative chemisorption were further calculated with the three DFs. For H₂, rMS-RPBEL-rVV10 is 0.10 eV closer to the benchmark value of 0.63 eV^{25,69} than RPBE-D3. BEEF-vdW overestimates the barrier by 0.31 eV. It also fails in predicting the CO₂ dissociation barrier, i.e., the BEEF-vdW value is the furthest away from the reference value. This can likely be ascribed to inaccuracies in addressing the O–C–O backbone in the BEEF-vdW functional. The value predicted by rMS-RPBEL-rVV10 is closest to the reference value. It has to be noted that the reference value for CO₂ dissociation is the energy barrier for dissociation on a Cu(100) surface and only serves to give an indication of the barrier height as, to the best of our knowledge, there is no suitable reference value on Cu(111) in

literature. Hence, we did not include the CO₂ dissociation barrier energies in the calculation of the mean signed deviation (MSD) and the mean absolute deviation (MAD) in Table 1.

Dissociative adsorption of O₂ onto the Cu(111) surface has been a topic of debate, mainly because O₂ has triplet spin in its ground state.⁷⁰ Helium atom scattering experiments⁷¹ have indicated an energy barrier for O₂ dissociation on the Cu(111) surface, while DFT calculations using GGA-level DFs often predict it as a spontaneous process.⁷² The transition from the triplet state to the singlet state often introduces inaccuracies in the description of the electronic density with GGA-level DFs, leading to a rather poor description of the activated character.⁷³ Notably, the dimer method for TS search proved ineffective for RPBE-D3 and BEEF-vdW DFs. Hence, we constructed 2D cuts of the 6D potential energy surface (PES) by varying the O₂-surface distance and O–O bond length on the bridge site of Cu(111) with the three DFs. Figure S6 shows these elbow plots. From the elbow plots, it is clear that there is no barrier predicted by RPBE-D3 and BEEF-vdW. In contrast, the rMS-RPBE-rVV10 elbow plot demonstrates a noticeable energy barrier between the physisorption well at higher distances from the surface and the dissociative chemisorption well at lower distances from the surface and higher O–O bond lengths. Although the absolute energy of the top of the barrier is slightly lower, i.e., −0.05 eV, than the reference energy of O₂ and the surface far away from each other, it offers a qualitatively more accurate description compared to GGA-level DFs as they predict no barrier at all. As both RPBE-D3 and BEEF-vdW do not predict a barrier, O₂ dissociation was not included in Table 1 and the calculation of the MSD and MAD. We also note that, in general, the MS DFs yield superior performance so far over GGA DFs for the prediction of barrier heights for systems that exhibit a large amount of charge transfer.^{6,32} Hence, rMS-RPBE-rVV10 seems to outperform GGA DFs in predicting molecule–metal surface reaction barriers.

Based on the tabulated values, the MSD values for the RPBE-D3, BEEF-vdW, and rMS-RPBE-rVV10 are determined to be −0.08, 0.15, and 0.02 eV, respectively. The MAD values corresponding to these DFs are calculated to be 0.11, 0.17, and 0.15 eV, respectively. In general, the GGA-DFs with vdW corrections, especially RPBE-D3, perform similar to rMS-RPBE-rVV10 for adsorption energies but fail at predicting barriers for dissociation, aligning with the consensus that GGA DFs systematically get the barriers wrong.⁶ Correctly predicting these barriers is crucial for the development of a metal surface reaction network. Hence, we propose that for intricate reaction networks such as CO₂, hydrogenation to CH₃OH rMS-RPBE-rVV10 demonstrates superior predictive capabilities with respect to GGA DFs. This mGGA-level DF with vdW correction likely attains a reasonable level of prediction by partially mitigating the SIE as well as by distinguishing the molecular and metallic regimes.

In order to further evaluate the performance of rMS-RPBE-rVV10 for the CO₂ reaction network, we make a comparison with state-of-the-art studies including van der Waals (vdW) corrections. For the formate pathway on Cu(111), we compare our rMS-RPBE-rVV10 results with the results of Shi et al.,⁷⁴ who employed the PBE-D3 DF (Figure 3a), since RPBE-D3 results are missing from literature. For the formate pathway on Cu(211), we compare our results to those of Studt et al.,²¹ who employed the BEEF-vdW DF (Figure 3b). All of the corrections, i.e., empirical energy corrections for gas-phase

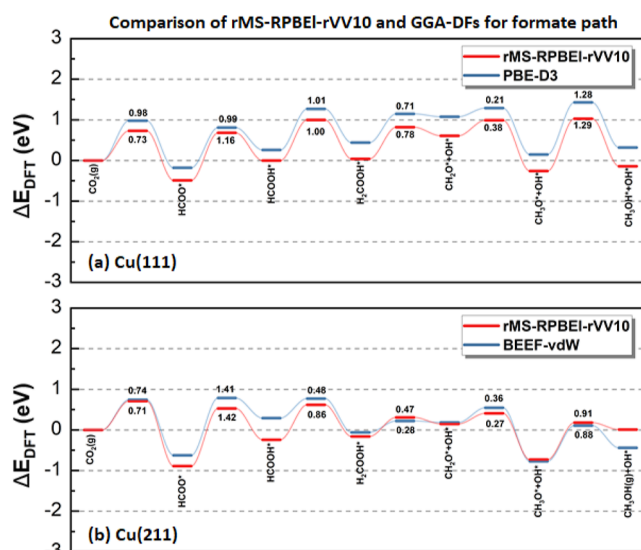


Figure 3. Potential energy diagram for the optimal formate pathway computed with (a) PBE-D3 (blue) and rMS-RPBE-rVV10 (red) on Cu(111) and (b) BEEF-vdW (blue) and rMS-RPBE-rVV10 (red) on Cu(211). To simplify, H* are not listed. Activation energy barriers are denoted in eV.

molecules that have an O–C–O bond, are removed for a clear comparison.

Both PBE-D3 and rMS-RPBE-rVV10 predict that the process's highest activation barrier on Cu(111) occurs during the hydrogenation of CH₃O* to CH₃OH*. It is important to note that the majority of the reaction barriers calculated using rMS-RPBE-rVV10 tend to be marginally higher than those obtained with PBE-D3. As discussed earlier, this discrepancy may be ascribed to the difficulties GGA DFs have in predicting reaction barriers. However, an exception can be observed in the reaction step CO₂(g) + H* → HCOO*, which might involve the difference of the description of gas-phase molecules by both DFs.

In contrast to Cu(111), on Cu(211), BEEF-vdW and rMS-RPBE-rVV10 both predict HCOO* hydrogenation to have the highest barrier. Note that the results published by Studt et al. contain empirical corrections, which we removed here.¹⁷ Overall, rMS-RPBE-rVV10 again predicts higher energy barriers than BEEF-vdW.

3.2. Analysis of CH₃OH Formation Pathways. Finally, we compare the three different pathways on Cu(111) and Cu(211) computed with rMS-RPBE-rVV10 in Figure 4. A more detailed discussion of all possible pathways can be found in S.6 in the Supporting Information. On Cu(111), the formate path proceeds through HCOO* rather than H₂COO* and the carboxyl path through CO* rather than COHO*. The rate-controlling steps for each path are indicated in Figure 4a. Based on the rate-controlling step, the formate and CO₂ dissociation pathways are equally favorable as the highest barriers have the same height for both paths and are lower than the highest barrier in the carboxyl path. The CO₂ dissociation has two possible rate-controlling steps that have the same barrier, namely, CO₂* dissociation and CH₃O* hydrogenation; both TSs are depicted in the figure. As the rate-controlling barriers in the CO₂ dissociation pathway and formate pathway are the same height, it is difficult to draw a conclusion about the most favorable pathways on Cu(111). These results underline the importance of the DF as the small differences

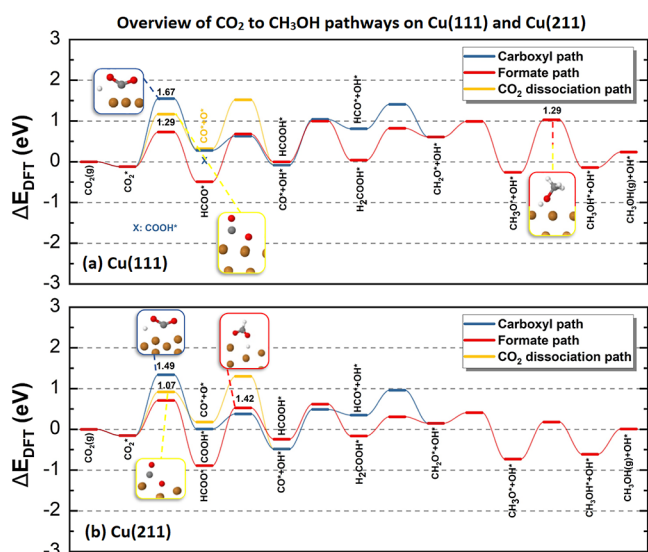


Figure 4. Potential energy diagram of possible CO₂ hydrogenation pathways on (a) Cu(111) and (b) Cu(211) computed with rMS-RPBE-rVV10. The carboxyl path is in blue, the formate path is in red, and the CO₂ dissociation path is in yellow. To simplify, all H* are not listed. TS geometries of the rate-controlling step and their energy (in eV) for each pathway, as well as intermediate states, are depicted in the figure.

due to the choice of DF between pathways can easily change their relative importance.

On Cu(211), the formate and the carboxyl path proceed through the same intermediates as on Cu(111). The rate-controlling step for the formate route is the hydrogenation of HCOO* to HCOOH*, which is different from the rate-controlling step on Cu(111), namely, CH₃O* hydrogenation. The rate-controlling step in the carboxyl path is the formation of COOH*, the same as on Cu(111). For the CO₂ dissociation pathway, CO₂* dissociation is the rate-controlling step, again the same as on Cu(111). Based on the rate-controlling step, the CO₂ dissociation pathway is the most favorable on Cu(211) as it has the lowest rate-controlling barrier.

In general, the intermediate states are more stable, relative to gaseous CO₂, on Cu(211) than on Cu(111), and the reaction barriers are lower on Cu(211). This is illustrated in Figure S13 for the formate pathway. The mean difference in activation energy barriers for all elementary reactions in the three pathways leading to CH₃OH formation, calculated as $E_a(111) - E_a(211)$, is 0.13 eV. This indicates that, in general, the differences are small and that there are important exceptions like the hydrogenation of HCOO*, which has a higher barrier on Cu(211).

The experimental affirmation of a CO promotion effect, as indicated by our calculations that point to the importance of CO in the CO₂ dissociation path on both facets, in the synthesis of methanol from a CO₂/H₂ mixture is well-accepted, yet the reason for this effect remains unclear. It has been suggested that this effect is due to CO promoting HCOO* hydrogenation.⁷⁵ Other studies posit that the CO concentration in the gas phase could enhance morphological modifications on the catalyst particles that can potentially explain the observed promotion effect on catalytic activity.⁷⁶ Both of the former mechanisms are, of course, not captured by our DFT calculations. It is worth noting that the highest energy barrier in the formate pathway on the Cu(211) surface

occurs in the hydrogenation of HCOO* to HCOOH*. In contrast, for the formate path on the Cu(111) surface, the highest energy barrier occurs in the hydrogenation of CH₃O* to CH₃OH*. Experiments confirmed the presence of surface HCOO* during CO₂ hydrogenation to methanol on several Cu-based catalysts.^{77,78} Furthermore, similar to HCOO*, infrared experiments revealed the presence of CH₃O* on Cu-based catalysts.^{54,77} Edwards and Schrader⁷⁵ determined through in situ infrared testing that the hydrogenation of CH₃O* on Cu-based catalyst surfaces is the rate-controlling step for CH₃OH production, similar to our results on Cu(111). The presence of these intermediates is something that would be expected on the basis of our calculations, i.e., the hydrogenation of CH₃O* is a rate-controlling step on Cu(111) and HCOO* is the most stable intermediate, relative to gas-phase CO₂, on Cu(211) and has the second highest barrier to be hydrogenated on Cu(211).

From the discussion above, we cannot draw any definite conclusion about which pathway is responsible for CO₂ conversion to CH₃OH on either Cu surface. For example, the CO₂ dissociation pathway has the lowest rate-controlling barrier on Cu(211) but goes through HCO*, which is kinetically unstable, as it is likely to react back to H* and CO* because this reaction has a lower barrier than that of hydrogenation to CH₂O*. Furthermore, several intermediates, like CH₂O*, are only weakly adsorbed, and desorption of these intermediates could influence the mechanism. It is hard, if not impossible, to draw a conclusion about the pathways based on DFT data alone. We plan to construct a microkinetic model to analyze the reaction network in more detail as all these different aspects can be included in such a model. Nevertheless, our DFT calculations do provide valuable insights, and it is the first time, to the best of our knowledge, that all these pathways are investigated in one study. Some of the studies mentioned in this paper only study one pathway, and most of them do not include CO₂ dissociation, which, according to our calculations, is the most favorable pathway on Cu(211). It is also the first time that this system is investigated with a mGGA DF, which should indeed yield more robust results than with GGA DFs. We emphasize that it is important that the employed DF is relatively robust with respect to the various pathways for the calculations to be able to make predictions.

4. CONCLUSIONS

In summary, this study investigates for the first time the performance of a mGGA-level DF in predicting reaction networks on a metal surface. We compare the new rMS-RPBE-rVV10 mGGA DF with the representative (R)PBE-D3 and BEEF-vdW GGA DFs using the catalytically important CO₂ hydrogenation process on the Cu(111) and Cu(211) surfaces. The calculation of ΔG for CO and CO₂ hydrogenation in the gas phase shows that rMS-RPBE-rVV10 provides the closest prediction to the reference value for ΔG_{CO₂}, without requiring empirical corrections for a qualitatively correct description, which has been typically a necessity with GGA DFs so far. Furthermore, the adsorption and activation energies of various intermediates and reactions on Cu(111) are investigated. All three DFs predict similar adsorption and TS geometries but show discrepancies in the adsorption and activation energies. While RPBE-D3 has the lowest MAD (0.11 eV), rMS-RPBE-rVV10 also yields low MSD and MAD (0.02 and 0.15 eV, respectively). rMS-RPBE-

rVV10 performs similarly to the GGA DFs for adsorption but performs significantly better in predicting dissociation barriers, which are often critical in reaction networks. Together with the improved description of gas-phase molecules compared to GGA DFs and the similar performance for the prediction of adsorption energies and lattice constants, this indicates an outstanding performance of the mGGA DF for reaction networks. By comparing to other state-of-the-art studies, particularly for the formate pathways on the Cu(111) and Cu(211) surfaces, we find that rMS-RPBEL-rVV10 generally predicts higher energy barriers for surface reactions than GGA-level DFs and shows promise for more accurate predictions of CO₂ hydrogenation processes. Also, by comparing different reaction pathways, we show that it is important for a DF to yield robust performance across a reaction network as the relative importance of pathways can be dependent on the choice of level of theory of the DF. This is in contrast to choosing a different DF at the same level of theory as the barriers will be shifted in a similar way in that case, not altering the relative importance. For example, our rMS-RPBEL-rVV10 results show that CO₂ dissociation is one of the most favorable pathways on Cu(211), while typical GGA DF-level studies in literature dismiss this pathway. However, definitive conclusions regarding the CO₂ conversion pathway to CH₃OH on Cu(211) or Cu(111) surfaces require further analysis using a microkinetic model. Unfortunately, rMS-RPBEL-rVV10 does not resolve the “CO adsorption puzzle”, illustrating the need for the development of hybrid mGGA DFs that solve the SIE. Likewise, development of a more advanced vdW DF that takes advantage of the KED to supplement a (hybrid) mGGA DF should yield a considerable improvement over the employed rVV10 nonlocal correlation DF. In short, the use of a mGGA DF yields superior performance over GGA DFs for catalytically relevant reaction networks on metal surfaces. Considering the reasonable increase of computational cost, up to a factor of three, we recommend that future development of state-of-the-art reaction networks makes use of mGGA DFs instead of GGA DFs as mGGA DFs significantly improve the description of the gas phase and reaction barriers.

■ ASSOCIATED CONTENT

SI Supporting Information

The Supporting Information is available free of charge at <https://pubs.acs.org/doi/10.1021/acs.jpcc.4c01110>.

Convergence of computational parameters for HCOOH adsorption energy; formulas for the calculation of Gibbs free energy; adsorption energy and adsorption sites for all intermediates on Cu(111) and Cu(211) calculated with rMS-RPBEL-rVV10; list of (adsorbed) species and corresponding energies, entropies, zero-point energy, and thermal corrections calculated with rMS-RPBEL-rVV10, BEEF-vdW, and RPBE-D3; 6D PES of O₂ dissociation on the Cu(111) surface; and detailed analysis of formate, carboxyl, and CO₂ dissociation pathways on Cu(111) and Cu(211) (PDF)

■ AUTHOR INFORMATION

Corresponding Author

Nick Gerrits – Research Group PLASMANT, Department of Chemistry, University of Antwerp, Antwerp, Wilrijk BE-2610, Belgium; Leiden Institute of Chemistry, Gorlaeus Laboratories, Leiden University, Leiden 2300 RA, The

Netherlands; orcid.org/0000-0001-5405-7860;

Email: n.gerrits@lic.leidenuniv.nl

Authors

Yuxiang Cai – Research Group PLASMANT, Department of Chemistry, University of Antwerp, Antwerp, Wilrijk BE-2610, Belgium; Department of Electrical Engineering and Electronics, University of Liverpool, Liverpool L69 3GJ, U.K.

Roel Michiels – Research Group PLASMANT, Department of Chemistry, University of Antwerp, Antwerp, Wilrijk BE-2610, Belgium

Federica De Luca – Research Group PLASMANT, Department of Chemistry, University of Antwerp, Antwerp, Wilrijk BE-2610, Belgium; Department of ChiBioFarAM (Industrial Chemistry), ERIC aisbl and INSTM/CASPE, University of Messina, Messina 98166, Italy

Erik Neyts – Research Group PLASMANT, Department of Chemistry, University of Antwerp, Antwerp, Wilrijk BE-2610, Belgium; orcid.org/0000-0002-3360-3196

Xin Tu – Department of Electrical Engineering and Electronics, University of Liverpool, Liverpool L69 3GJ, U.K.; orcid.org/0000-0002-6376-0897

Annemie Bogaerts – Research Group PLASMANT, Department of Chemistry, University of Antwerp, Antwerp, Wilrijk BE-2610, Belgium; orcid.org/0000-0001-9875-6460

Complete contact information is available at: <https://pubs.acs.org/10.1021/acs.jpcc.4c01110>

Author Contributions

¹Y.C. and R.M. were the first authors.

Notes

The authors declare no competing financial interest.

■ ACKNOWLEDGMENTS

N.G. has been financially supported through an NWO Rubicon grant (no. 019.202EN.012). R.M. has been financially supported through an FWO grant (no. 1114921N) and by the European Research Council (ERC) under the European Union's Horizon 2020 Research and Innovation programme (grant agreement no. 810182—SCOPE ERC Synergy project). Y.C. was supported by the European Union's Horizon 2020 Research and Innovation programme under the Marie Skłodowska-Curie grant agreement no. 813393 (PIONEER). The computational resources and services used in this work were provided by the VSC (Flemish Supercomputer Center), funded by the Research Foundation-Flanders (FWO) and the Flemish Government.

■ REFERENCES

- (1) Intergovernmental Panel On Climate Change (IPCC). *Climate Change 2021—The Physical Science Basis: Working Group I Contribution to the Sixth Assessment Report of the Intergovernmental Panel on Climate Change*, 1st ed.; Cambridge University Press, 2023.
- (2) Centi, G.; Quadrelli, E. A.; Perathoner, S. Catalysis for CO₂ Conversion: A Key Technology for Rapid Introduction of Renewable Energy in the Value Chain of Chemical Industries. *Energy Environ. Sci.* **2013**, *6* (6), 1711–1731.
- (3) Tameh, M. S.; Dearden, A. K.; Huang, C. Accuracy of Density Functional Theory for Predicting Kinetics of Methanol Synthesis from CO and CO₂ Hydrogenation on Copper. *J. Phys. Chem. C* **2018**, *122* (31), 17942–17953.
- (4) Peverati, R.; Truhlar, D. G. Quest for a Universal Density Functional: The Accuracy of Density Functionals across a Broad

Spectrum of Databases in Chemistry and Physics. *Philos. Trans. R. Soc., A* **2014**, *372* (2011), 20120476.

(5) Schimka, L.; Harl, J.; Stroppa, A.; Grüneis, A.; Marsman, M.; Mittendorfer, F.; Kresse, G. Accurate Surface and Adsorption Energies from Many-Body Perturbation Theory. *Nat. Mater.* **2010**, *9* (9), 741–744.

(6) Gerrits, N.; Smeets, E. W. F.; Vuckovic, S.; Powell, A. D.; Doblhoff-Dier, K.; Kroes, G.-J. Density Functional Theory for Molecule-Metal Surface Reactions: When Does the Generalized Gradient Approximation Get It Right, and What to Do If It Does Not. *J. Phys. Chem. Lett.* **2020**, *11* (24), 10552–10560.

(7) Sun, J.; Haunschild, R.; Xiao, B.; Bulik, I. W.; Scuseria, G. E.; Perdew, J. P. Semilocal and Hybrid Meta-Generalized Gradient Approximations Based on the Understanding of the Kinetic-Energy-Density Dependence. *J. Chem. Phys.* **2013**, *138* (4), 044113.

(8) Sun, J.; Ruzsinszky, A.; Perdew, J. P. Strongly Constrained and Appropriately Normed Semilocal Density Functional. *Phys. Rev. Lett.* **2015**, *115* (3), 036402.

(9) Tao, J.; Perdew, J. P.; Staroverov, V. N.; Scuseria, G. E. Climbing the Density Functional Ladder: Nonempirical Meta-Generalized Gradient Approximation Designed for Molecules and Solids. *Phys. Rev. Lett.* **2003**, *91* (14), 146401.

(10) Smeets, E. W. F.; Voss, J.; Kroes, G.-J. Specific Reaction Parameter Density Functional Based on the Meta-Generalized Gradient Approximation: Application to H₂ + Cu(111) and H₂ + Ag(111). *J. Phys. Chem. A* **2019**, *123* (25), 5395–5406.

(11) Odashima, M. M.; Capelle, K.; Trickey, S. B. Tightened Lieb–Oxford Bound for Systems of Fixed Particle Number. *J. Chem. Theory Comput.* **2009**, *5* (4), 798–807.

(12) Sun, J.; Xiao, B.; Fang, Y.; Haunschild, R.; Hao, P.; Ruzsinszky, A.; Csonka, G. I.; Scuseria, G. E.; Perdew, J. P. Density Functionals That Recognize Covalent, Metallic, and Weak Bonds. *Phys. Rev. Lett.* **2013**, *111* (10), 106401.

(13) Yang, Y.; Evans, J.; Rodriguez, J. A.; White, M. G.; Liu, P. Fundamental studies of methanol synthesis from CO₂ hydrogenation on Cu(111), Cu clusters, and Cu/ZnO(0001). *Phys. Chem. Chem. Phys.* **2010**, *12* (33), 9909–9917.

(14) Grabow, L. C.; Mavrikakis, M. Mechanism of Methanol Synthesis on Cu through CO₂ and CO Hydrogenation. *ACS Catal.* **2011**, *1* (4), 365–384.

(15) Yang, Y.; White, M. G.; Liu, P. Theoretical Study of Methanol Synthesis from CO₂ Hydrogenation on Metal-Doped Cu(111) Surfaces. *J. Phys. Chem. C* **2012**, *116* (1), 248–256.

(16) Zhao, Y.-F.; Yang, Y.; Mims, C.; Peden, C. H. F.; Li, J.; Mei, D. Insight into Methanol Synthesis from CO₂ Hydrogenation on Cu(111): Complex Reaction Network and the Effects of H₂O. *J. Catal.* **2011**, *281* (2), 199–211.

(17) Studt, F.; Behrens, M.; Kunkes, E. L.; Thomas, N.; Zander, S.; Tarasov, A.; Schumann, J.; Frei, E.; Varley, J. B.; Abild-Pedersen, F.; Nørskov, J. K.; Schlögl, R. The Mechanism of CO and CO₂ Hydrogenation to Methanol over Cu-Based Catalysts. *ChemCatChem* **2015**, *7* (7), 1105–1111.

(18) Zheng, H.; Narkhede, N.; Han, L.; Zhang, H.; Li, Z. Methanol Synthesis from CO₂: A DFT Investigation on Zn-Promoted Cu Catalyst. *Res. Chem. Intermed.* **2020**, *46* (3), 1749–1769.

(19) Zhang, X.; Liu, J.-X.; Zijlstra, B.; Filot, I. A. W.; Zhou, Z.; Sun, S.; Hensen, E. J. M. Optimum Cu Nanoparticle Catalysts for CO₂ Hydrogenation towards Methanol. *Nano Energy* **2018**, *43*, 200–209.

(20) Xu, D.; Wu, P.; Yang, B. Essential Role of Water in the Autocatalysis Behavior of Methanol Synthesis from CO₂ Hydrogenation on Cu: A Combined DFT and Microkinetic Modeling Study. *J. Phys. Chem. C* **2019**, *123* (14), 8959–8966.

(21) Studt, F.; Abild-Pedersen, F.; Varley, J. B.; Nørskov, J. K. CO and CO₂ Hydrogenation to Methanol Calculated Using the BEEF-vdW Functional. *Catal. Lett.* **2013**, *143* (1), 71–73.

(22) Wellendorff, J.; Lundgaard, K. T.; Møgelhøj, A.; Petzold, V.; Landis, D. D.; Nørskov, J. K.; Bligaard, T.; Jacobsen, K. W. Density Functionals for Surface Science: Exchange-Correlation Model

Development with Bayesian Error Estimation. *Phys. Rev. B: Condens. Matter Mater. Phys.* **2012**, *85* (23), 235149.

(23) Hammer, B.; Hansen, L. B.; Nørskov, J. K. Improved Adsorption Energetics within Density-Functional Theory Using Revised Perdew-Burke-Ernzerhof Functionals. *Phys. Rev. B: Condens. Matter Mater. Phys.* **1999**, *59* (11), 7413–7421.

(24) Garza, A. J.; Bell, A. T.; Head-Gordon, M. Nonempirical Meta-Generalized Gradient Approximations for Modeling Chemisorption at Metal Surfaces. *J. Chem. Theory Comput.* **2018**, *14* (6), 3083–3090.

(25) Tchakoua, T.; Gerrits, N.; Smeets, E. W. F.; Kroes, G.-J. SBH17: Benchmark Database of Barrier Heights for Dissociative Chemisorption on Transition Metal Surfaces. *J. Chem. Theory Comput.* **2023**, *19* (1), 245–270.

(26) Sun, J.; Xiao, B.; Ruzsinszky, A. Communication: Effect of the Orbital-Overlap Dependence in the Meta Generalized Gradient Approximation. *J. Chem. Phys.* **2012**, *137* (5), 051101.

(27) Perdew, J. P.; Burke, K.; Ernzerhof, M. Generalized Gradient Approximation Made Simple. *Phys. Rev. Lett.* **1996**, *77* (18), 3865–3868.

(28) Perdew, J. P.; Ruzsinszky, A.; Csonka, G. I.; Constantin, L. A.; Sun, J. Workhorse Semilocal Density Functional for Condensed Matter Physics and Quantum Chemistry. *Phys. Rev. Lett.* **2009**, *103* (2), 026403.

(29) Zhao, Y.; Truhlar, D. G. A New Local Density Functional for Main-Group Thermochemistry, Transition Metal Bonding, Thermochemical Kinetics, and Noncovalent Interactions. *J. Chem. Phys.* **2006**, *125* (19), 194101.

(30) Becke, A. D. On the Large-gradient Behavior of the Density Functional Exchange Energy. *J. Chem. Phys.* **1986**, *85* (12), 7184–7187.

(31) Perdew, J. P.; Ruzsinszky, A.; Csonka, G. I.; Vydrov, O. A.; Scuseria, G. E.; Constantin, L. A.; Zhou, X.; Burke, K. Restoring the Density-Gradient Expansion for Exchange in Solids and Surfaces. *Phys. Rev. Lett.* **2008**, *100* (13), 136406.

(32) Gerrits, N.; Geweke, J.; Smeets, E. W. F.; Voss, J.; Wodtke, A. M.; Kroes, G.-J. Closing the Gap Between Experiment and Theory: Reactive Scattering of HCl from Au(111). *J. Phys. Chem. C* **2020**, *124* (29), 15944–15960.

(33) Smeets, E. W. F.; Kroes, G.-J. Performance of Made Simple Meta-GGA Functionals with rVV10 Nonlocal Correlation for H₂ + Cu(111), D₂ + Ag(111), H₂ + Au(111), and D₂ + Pt(111). *J. Phys. Chem. C* **2021**, *125* (17), 8993–9010.

(34) Sabatini, R.; Gorni, T.; de Gironcoli, S. Nonlocal van Der Waals Density Functional Made Simple and Efficient. *Phys. Rev. B: Condens. Matter Mater. Phys.* **2013**, *87* (4), 041108.

(35) Wei, F.; Smeets, E. W. F.; Voss, J.; Kroes, G.-J.; Lin, S.; Guo, H. Assessing density functionals for describing methane dissociative chemisorption on Pt(110)-(2×1) surface. *Chin. J. Chem. Phys.* **2021**, *34*, 883–895.

(36) Furness, J. W.; Kaplan, A. D.; Ning, J.; Perdew, J. P.; Sun, J. Accurate and Numerically Efficient r2SCAN Meta-Generalized Gradient Approximation. *J. Phys. Chem. Lett.* **2020**, *11* (19), 8208–8215.

(37) Grimme, S.; Antony, J.; Ehrlich, S.; Krieg, H. A Consistent and Accurate Ab Initio Parametrization of Density Functional Dispersion Correction (DFT-D) for the 94 Elements H-Pu. *J. Chem. Phys.* **2010**, *132* (15), 154104.

(38) Kresse, G.; Hafner, J. Ab Initio Molecular Dynamics for Liquid Metals. *Phys. Rev. B: Condens. Matter Mater. Phys.* **1993**, *47* (1), 558–561.

(39) Kresse, G.; Hafner, J. Ab Initio Molecular-Dynamics Simulation of the Liquid-Metal-Amorphous-Semiconductor Transition in Germanium. *Phys. Rev. B: Condens. Matter Mater. Phys.* **1994**, *49* (20), 14251–14269.

(40) Kresse, G.; Furthmüller, J. Efficient Iterative Schemes for Ab Initio Total-Energy Calculations Using a Plane-Wave Basis Set. *Phys. Rev. B: Condens. Matter Mater. Phys.* **1996**, *54* (16), 11169–11186.

- (41) Kresse, G.; Furthmüller, J. Efficiency of Ab-Initio Total Energy Calculations for Metals and Semiconductors Using a Plane-Wave Basis Set. *Comput. Mater. Sci.* **1996**, *6* (1), 15–50.
- (42) Román-Pérez, G.; Soler, J. M. Efficient Implementation of a van Der Waals Density Functional: Application to Double-Wall Carbon Nanotubes. *Phys. Rev. Lett.* **2009**, *103* (9), 096102.
- (43) Klimeš, J.; Bowler, D. R.; Michaelides, A. Van Der Waals Density Functionals Applied to Solids. *Phys. Rev. B: Condens. Matter Mater. Phys.* **2011**, *83* (19), 195131.
- (44) Furness, J. W.; Sun, J. Enhancing the Efficiency of Density Functionals with an Improved Iso-Orbital Indicator. *Phys. Rev. B* **2019**, *99* (4), 041119.
- (45) Lee, K.; Murray, É. D.; Kong, L.; Lundqvist, B. I.; Langreth, D. C. Higher-Accuracy van Der Waals Density Functional. *Phys. Rev. B: Condens. Matter Mater. Phys.* **2010**, *82* (8), 081101.
- (46) Kresse, G.; Hafner, J. Norm-Conserving and Ultrasoft Pseudopotentials for First-Row and Transition Elements. *J. Phys.: Condens. Matter* **1994**, *6* (40), 8245–8257.
- (47) Kresse, G.; Joubert, D. From Ultrasoft Pseudopotentials to the Projector Augmented-Wave Method. *Phys. Rev. B: Condens. Matter Mater. Phys.* **1999**, *59* (3), 1758–1775.
- (48) Haas, P.; Tran, F.; Blaha, P. Calculation of the Lattice Constant of Solids with Semilocal Functionals. *Phys. Rev. B: Condens. Matter Mater. Phys.* **2009**, *79* (8), 085104.
- (49) Henkelman, G.; Jónsson, H. A Dimer Method for Finding Saddle Points on High Dimensional Potential Surfaces Using Only First Derivatives. *J. Chem. Phys.* **1999**, *111* (15), 7010–7022.
- (50) Heyden, A.; Bell, A. T.; Keil, F. J. Efficient Methods for Finding Transition States in Chemical Reactions: Comparison of Improved Dimer Method and Partitioned Rational Function Optimization Method. *J. Chem. Phys.* **2005**, *123* (22), 224101.
- (51) Kästner, J.; Sherwood, P. Superlinearly Converging Dimer Method for Transition State Search. *J. Chem. Phys.* **2008**, *128* (1), 014106.
- (52) Xiao, P.; Sheppard, D.; Rogal, J.; Henkelman, G. Solid-State Dimer Method for Calculating Solid-Solid Phase Transitions. *J. Chem. Phys.* **2014**, *140* (17), 174104.
- (53) Peterson, A. A.; Abild-Pedersen, F.; Studt, F.; Rossmeisl, J.; Nørskov, J. K. How Copper Catalyzes the Electroreduction of Carbon Dioxide into Hydrocarbon Fuels. *Energy Environ. Sci.* **2010**, *3* (9), 1311–1315.
- (54) Hinch, B. J.; Dubois, L. H. First-Order Corrections in Modulated Molecular Beam Desorption Experiments. *Chem. Phys. Lett.* **1990**, *171* (1–2), 131–135.
- (55) Thiel, P. A.; Madey, T. E. The Interaction of Water with Solid Surfaces: Fundamental Aspects. *Surf. Sci. Rep.* **1987**, *7* (6–8), 211–385.
- (56) Shiozawa, Y.; Koitaya, T.; Mukai, K.; Yoshimoto, S.; Yoshinobu, J. Quantitative Analysis of Desorption and Decomposition Kinetics of Formic Acid on Cu(111): The Importance of Hydrogen Bonding between Adsorbed Species. *J. Chem. Phys.* **2015**, *143* (23), 234707.
- (57) Greeley, J.; Mavrikakis, M. Methanol Decomposition on Cu(111): A DFT Study. *J. Catal.* **2002**, *208* (2), 291–300.
- (58) Koitaya, T.; Shiozawa, Y.; Yoshikura, Y.; Mukai, K.; Yoshimoto, S.; Yoshinobu, J. Systematic Study of Adsorption and the Reaction of Methanol on Three Model Catalysts: Cu(111), Zn-Cu(111), and Oxidized Zn-Cu(111). *J. Phys. Chem. C* **2017**, *121* (45), 25402–25410.
- (59) Muttaqien, F.; Hamamoto, Y.; Hamada, I.; Inagaki, K.; Shiozawa, Y.; Mukai, K.; Koitaya, T.; Yoshimoto, S.; Yoshinobu, J.; Morikawa, Y. CO₂ Adsorption on the Copper Surfaces: Van Der Waals Density Functional and TPD Studies. *J. Chem. Phys.* **2017**, *147* (9), 094702.
- (60) Andersson, S.; Persson, M. Sticking in the Physisorption Well: Influence of Surface Structure. *Phys. Rev. Lett.* **1993**, *70* (2), 202–205.
- (61) Rasmussen, P. B.; Taylor, P. A.; Chorkendorff, I. The Interaction of Carbon Dioxide with Cu(100). *Surf. Sci.* **1992**, *269*–270, 352–359.
- (62) Zuo, Z.-J.; Wang, L.; Han, P.-D.; Huang, W. Methanol Synthesis by CO and CO₂ Hydrogenation on Cu/ γ -Al₂O₃ Surface in Liquid Paraffin Solution. *Appl. Surf. Sci.* **2014**, *290*, 398–404.
- (63) Gokhale, A. A.; Dumesic, J. A.; Mavrikakis, M. On the Mechanism of Low-Temperature Water Gas Shift Reaction on Copper. *J. Am. Chem. Soc.* **2008**, *130* (4), 1402–1414.
- (64) Neef, M.; Doll, K. CO Adsorption on the Cu(111) Surface: A Density Functional Study. *Surf. Sci.* **2006**, *600* (5), 1085–1092.
- (65) Feibelman, P. J.; Hammer, B.; Nørskov, J. K.; Wagner, F.; Scheffler, M.; Stumpf, R.; Watwe, R.; Dumesic, J. The CO/Pt(111) Puzzle. *J. Phys. Chem. B* **2001**, *105* (18), 4018–4025.
- (66) Kessler, J.; Thieme, F. Chemisorption of CO on Differently Prepared Cu(111) Surfaces. *Surf. Sci.* **1977**, *67* (2), 405–415.
- (67) Patra, A.; Peng, H.; Sun, J.; Perdew, J. P. Rethinking CO Adsorption on Transition-Metal Surfaces: Effect of Density-Driven Self-Interaction Errors. *Phys. Rev. B* **2019**, *100* (3), 035442.
- (68) Mishima, K.; Kaneko, M.; Song, J.-W.; Kawai, H.; Yamashita, K.; Hirao, K. Application of Accelerated Long-Range Corrected Exchange Functional [LC-DFT(2Gau)] to Periodic Boundary Condition Systems: CO Adsorption on Cu(111) Surface. *J. Chem. Phys.* **2020**, *152* (10), 104105.
- (69) Díaz, C.; Pijper, E.; Olsen, R. A.; Busnengo, H. F.; Auerbach, D. J.; Kroes, G. J. Chemically Accurate Simulation of a Prototypical Surface Reaction: H₂ Dissociation on Cu(111). *Science* **2009**, *326* (5954), 832–834.
- (70) Behler, J.; Delley, B.; Lorenz, S.; Reuter, K.; Scheffler, M. Dissociation of O₂ at Al(111): The Role of Spin Selection Rules. *Phys. Rev. Lett.* **2005**, *94* (3), 036104.
- (71) Minniti, M.; Fariás, D.; Perna, P.; Miranda, R. Enhanced Selectivity towards O₂ and H₂ Dissociation on Ultrathin Cu Films on Ru(0001). *J. Chem. Phys.* **2012**, *137* (7), 074706.
- (72) Xu, Y.; Mavrikakis, M. Adsorption and dissociation of O₂ on Cu(): thermochemistry, reaction barrier and the effect of strain. *Surf. Sci.* **2001**, *494* (2), 131–144.
- (73) Ramos, M.; Díaz, C.; Martínez, A. E.; Busnengo, H. F.; Martín, F. Dissociative and Non-Dissociative Adsorption of O₂ on Cu(111) and CuML/Ru(0001) Surfaces: Adiabaticity Takes Over. *Phys. Chem. Chem. Phys.* **2017**, *19* (16), 10217–10221.
- (74) Shi, Y.-F.; Kang, P.-L.; Shang, C.; Liu, Z.-P. Methanol Synthesis from CO₂/CO Mixture on Cu-Zn Catalysts from Microkinetics-Guided Machine Learning Pathway Search. *J. Am. Chem. Soc.* **2022**, *144* (29), 13401–13414.
- (75) Edwards, J. F.; Schrader, G. L. Infrared Spectroscopy of Copper/Zinc Oxide Catalysts for the Water-Gas Shift Reaction and Methanol Synthesis. *J. Phys. Chem.* **1984**, *88* (23), S620–S624.
- (76) Hansen, P. L.; Wagner, J. B.; Helveg, S.; Rostrup-Nielsen, J. R.; Clausen, B. S.; Topsøe, H. Atom-Resolved Imaging of Dynamic Shape Changes in Supported Copper Nanocrystals. *Science* **2002**, *295* (5562), 2053–2055.
- (77) Clarke, D. B.; Bell, A. T. An Infrared Study of Methanol Synthesis from CO₂ on Clean and Potassium-Promoted Cu/SiO₂. *J. Catal.* **1995**, *154* (2), 314–328.
- (78) Fujitani, T.; Nakamura, I.; Uchijima, T.; Nakamura, J. The Kinetics and Mechanism of Methanol Synthesis by Hydrogenation of CO₂ over a Zn-Deposited Cu(111) Surface. *Surf. Sci.* **1997**, *383* (2–3), 285–298.