Almost complex structures, transverse complex structures, and (p,0) Dolbeault cohomology

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An almost complex structure j on a manifold M is integrable if and only if its Nijenhuis tensor N^j vanishes, and this is true iff the distribution $T_j^{\{1,0\}} \subset TM^C$ is involutive.

When it is not integrable, we relate properties of M to properties of distributions associated to j. In particular, we study conditions for j to define a complex tranverse structure and we relate the transverse (p, 0) Dolbeault cohomology to the (p, 0) generalized Dolbeault cohomology of (M, j) as introduced recently by Cirici and Wilson.